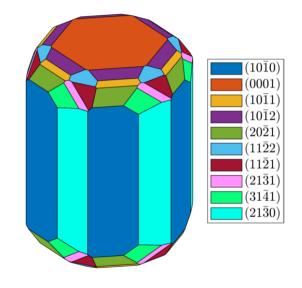
Matlab Basics and General Concepts of the MTEX Toolbox

R. Hielscher

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2021

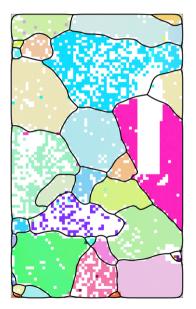
- crystal geometry
- ► EBSD data
- grains, grain boundaries
- XRD data
- orientation distribution function
- texture simulations
- tensorial properties
- elastic / plastic deformation
- misorientations / twinning
- phase transformations
- parent grain reconstruction



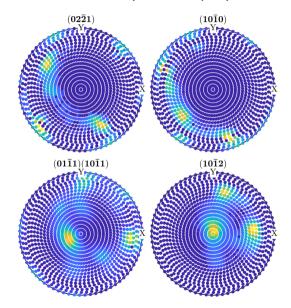
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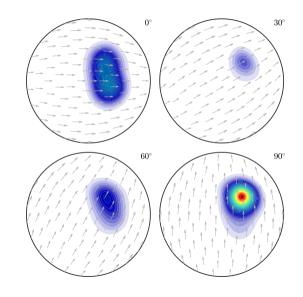
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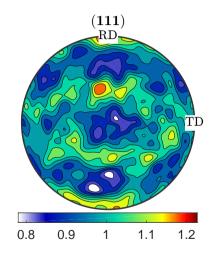
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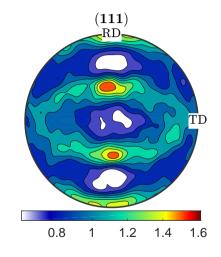
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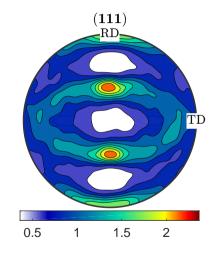
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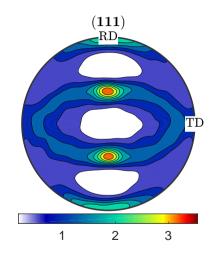
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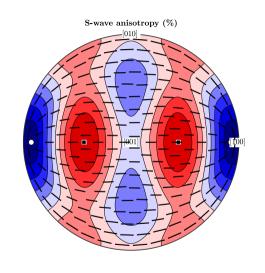
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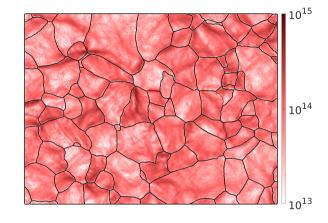
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Focus: basics, generality, speed

MTEX an Open Source Toolbox

Large, well documented, tested

- ▶ 13 years of development
- ▶ 40 000 lines of code, 33 percent comments
- ▶ 2000 downloads per version
- ·

- ▶ 1000 functions
- ▶ 14 reference paper, about 2000 references
- ► 1000 help pages
- ▶ add-ons: MTEX GUI, MTEX2Gmsh, Stabix, CrystalAligner, phaseSegmenter

A Teaching Tool

- everything can be visualized
- everything can be combined with everything
- everything can be manipulated

- Free and open software
 - ▶ free to use

► free to modify

very nice comunity

```
MTEX - A Matlab based scripting language
% load data
ebsd = EBSD. load('Emsland_plessite.ctf')
% plot data
plot(ebsd('Fe'), ebsd('Fe'). orientations)
% reconstruct grains
```

th = 5*degree: grains = calcGrains(ebsd, 'threshold',th) % find largest grain [m, id] = max(grains.area)% plot largest grain plot(grains(id).boundary, 'linewidth',2)

MTEX - A Matlab based scripting language

```
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th = 5*degree:
grains = calcGrains(ebsd, 'threshold',th)
% find largest grain
[m, id] = max(grains.area)
% plot largest grain
plot(grains(id).boundary, 'linewidth',2)
```

Why scripts?

- reproducible results
- easy to document
- templates for common tasks
- extensively customizable
 - batch processing of many data sets
 - repeated calculations with different parameters

Best practice

avoid loops

- comment your scripts
- ► short scripts
- ▶ function for repeated tasks

MTEX Resources

- **▶** documentation
- ▶ function reference
- examples
- user scripts
- ▶ discussion forum

Matlab

centered around matrices

Three dimensional vectors are given by there coordinates with respect to a orthogonal coordinate system $\vec{X}, \vec{Y}, \vec{Z}$

$$\vec{r} = x \cdot \vec{X} + y \cdot \vec{Y} + z \cdot \vec{Z}$$

For general vectors, MTEX does **not** care about the coordinate system, but works only with the coordinates.

$$r = \mathbf{vector3d}(1,2,3)$$

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For general vectors, MTEX does **not** care about the coordinate system, but works only with the coordinates.

```
r = vector3d(1,2,3)
r = vector3d (show methods, plot)
size: 1 x 1
x y z
1 2 3
```

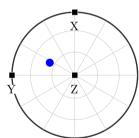
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$$r = vector3d(1,2,3)$$

The alignment of the coordinate system is only important when plotting data



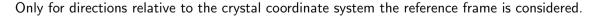
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$$r = vector3d(1,2,3)$$

The alignment of the coordinate system is only important when plotting data



predefined vectors

vector3d.X, vector3d.Y, vector3d.Z

```
polar coordinates \vec{r} = (\sin \theta \cos \rho, \sin \theta \sin \rho, \cos \theta)^t
```

theta = 90 * degree; rho = 45 * degree; r = vector3d.byPolar(theta,rho)

0

In MTEX all angles are in radiant!

combine vectors

$$r = [vector3d.X, vector3d.Y, vector3d(1,1,1)]$$

importing vectors

$$r = vector3d.load('file', 'ColumnNames', \{'x', 'y', 'z'\})$$

random vectors

```
r = vector3d.rand(100)
```

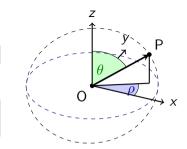
predefined vectors

vector3d.X, vector3d.Y, vector3d.Z

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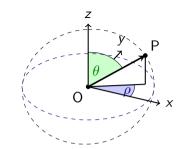
```
r = vector3d.byPolar(theta, rho)
```



combine vectors

```
r = [vector3d.X, vector3d.Y, vector3d(1,1,1)]
```

```
r = vector3d (show methods, plot)
size: 1 x 3
x y z
1 0 0
0 1 0
1 1 1
```

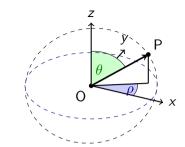


predefined vectors

vector3d.X, vector3d.Y, vector3d.Z

```
polar coordinates \vec{r} = (\sin \theta \cos \rho, \sin \theta \sin \rho, \cos \theta)^t
```

```
theta = 90 * degree; rho = 45 * degree;
r = vector3d.byPolar(theta,rho)
```



In MTEX all angles are in radiant!

combine vectors

$$r = [vector3d.X, vector3d.Y, vector3d(1,1,1)]$$

importing vectors

$$r = vector3d.load('file', 'ColumnNames', \{'x', 'y', 'z'\})$$

```
r = vector3d (show methods, plot)
  size: 200 x 1
```

predefined vectors

vector3d.X, vector3d.Y, vector3d.Z

polar coordinates $\vec{r} = (\sin \theta \cos \rho, \sin \theta \sin \rho, \cos \theta)^t$

theta = 90 * degree; rho = 45 * degree;

r = vector3d.byPolar(theta, rho)



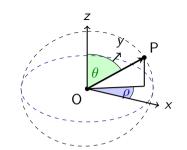
combine vectors

$$r = [vector3d.X, vector3d.Y, vector3d(1,1,1)]$$

importing vectors

random vectors

r = vector3d.rand(100)



Vector Calculations

```
simple algebra
```

```
r = 2*vector3d.X - vector3d.Y;
```

```
basic operation
```

```
cross(v1,v2) % dot product
cross(v1,v2) % cross product
angle(v1,v2) % angle between two vectors
normalize(v) % scale to norm 1
orth(v) % arbitrary orthogonal vector
```

```
r.theta % polar angle in radiant
```

```
r.rho % azimuth angle in radiant
r.x, r.y, r.z
```

Vector Calculations

```
simple algebra
```

```
r = 2*vector3d.X - vector3d.Y;
```

basic operations

```
dot(v1,v2)  % dot product
cross(v1,v2) % cross product
angle(v1,v2) % angle between two vectors
normalize(v) % scale to norm 1
orth(v)  % arbitrary orthogonal vector
```

extr

```
r.theta % polar angle in radiant
r.rho % azimuth angle in radiant
r x r y r z
```

Vector Calculations

```
simple algebra r = 2*vector3d.X - vector3d.Y;
```

```
basic operations

dot(v1,v2) % dot product
```

```
cross(v1,v2) % cross product
angle(v1,v2) % angle between two vectors
normalize(v) % scale to norm 1
```

extract properties
r.theta % polar angle in radiant

```
r.rho % azimuth angle in radiant r.x, r.y, r.z
```

orth(v) % arbitrary orthogonal vector

Indexing of Vectors

consider a list of vectors

```
r = vector3d ([0 0 1 1],[1 0 1 1],[1 1 1 0]);

r = vector3d (show methods, plot)
size: 1 x 4
x y z
0 1 1
0 0 1
1 1 1
1 1 0

single out the second vector
```

single out the second and the fourth vector

single out vectors by a logical condition

logical condition

Indexing of Vectors

consider a list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 0]);
```

single out the second vector

```
r = <u>vector3d</u> (show methods, plot)
size: 1 x 1
x y z
0 0 1
```

single out the second and the fourth vector

```
r([2 4])
```

r (2)

single out vectors by a logical condition

```
r(r.x>0)
```

The above techniques applies also to lists of rotations, orientations, tensors, EBSD data,

Indexing of Vectors

consider a list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 0]);
```

single out the second vector

```
r(2)
```

single out the second and the fourth vector

```
r([2 4])

r = vector3d (show methods, plot)
size: 1 x 2
x y z
0 0 1
1 1 0
```

single out vectors by a logical condition

```
r(r.x>0
```

The above techniques applies also to lists of rotations, orientations, tensors, ERSD data

Indexing of Vectors

consider a list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 0]);
```

single out the second vector

```
r(2)
```

single out the second and the fourth vector

```
r([2 4])
```

single out vectors by a logical condition

```
r(r.x>0)
r = vector3d (show methods, plot)
size: 1 x 2
x y z
1 1 1
1 1 0
```

Indexing of Vectors

consider a list of vectors

```
r = \mathbf{vector3d}([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 1 \ 0]);
```

single out the second vector

```
single out the second and the fourth vector
```

```
r([2 4])
```

r(2)

single out vectors by a logical condition

```
r(r.x>0)
```

The above techniques applies also to lists of rotations, orientations, tensors, EBSD data, grains, boundary segments, triple points, etc.

consider again the list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 1 \ 0]);
r = vector3d (show methods, plot)
  size · 1 x 4
```

r(2) = vector3d.Y

r(2) = vector3d.Y

consider again the list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 1 \ 0]);
```

replace the second vector by another vector

```
r = vector3d (show methods, plot)
size: 1 x 4
x y z
0 1 1
0 1 0
1 1 1
1 1 0
```

remove the second vector completely

change the x coordinate of all vectors

$$r.x = 0$$

consider again the list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 0]);
```

replace the second vector by another vector

```
r(2) = vector3d.Y
```

remove the second vector completely

```
r(2) = []
r = vector3d (show methods, plot)
size: 1 x 3
0 1 1
1 1 1
1 1 0
```

change the x coordinate of all vectors

```
r.x = 0
```

The above techniques applies also to pole figure data exionsations. ERSD data grains ats

consider again the list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 0]);
```

replace the second vector by another vector

```
r(2) = vector3d.Y
```

remove the second vector completely

```
r(2) = []
```

change the x coordinate of all vectors

```
r.x = 0
```

```
r = vector3d (show methods, plot)
size: 1 x 3
0 1 1
0 1 1
0 1 0
```

consider again the list of vectors

```
r = vector3d([0 \ 0 \ 1 \ 1],[1 \ 0 \ 1 \ 1],[1 \ 1 \ 1 \ 0]);
```

replace the second vector by another vector

```
r(2) = vector3d.Y
```

remove the second vector completely

$$r(2) = []$$

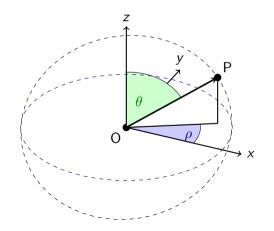
change the x coordinate of all vectors

```
r.x = 0
```

The above techniques applies also to pole figure data, orientations, EBSD data, grains, etc.

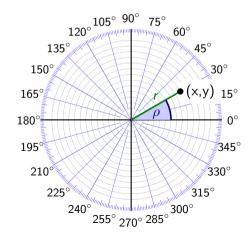
spherical polar coordinates

$$(x, y, z) = (\cos \rho \sin \theta, \sin \rho \sin \theta, \cos \theta)$$



polar coordinates in the plane

$$(x,y) = (r\cos\rho, r\sin\rho)$$



name	formula	schema
orthographic	$r = \sin \theta$	
equal angle (stereographic)	$r= anrac{ heta}{2}$	(1010)
gnonomic	r= an heta	$(01\overline{1}0) \underbrace{(01\overline{1}1)}_{(01\overline{1}1)} \underbrace{(01\overline{1}0)}_{(11\overline{0}0)} \underbrace{(01\overline{1}0)}_{(11\overline{0}1)}$
equal area (Schmidt)	$\sqrt{2(1-\cos\theta)}$	$(\overline{1211}) \qquad (0001) \qquad (1\overline{2}11) \\ (\overline{1101}) \qquad (0\overline{11}1) \qquad (0\overline{1}11) \\ (\overline{1100}) \qquad (0\overline{110})$
equal distant	$r = \theta$	$(\bar{1}100) \\ (\bar{2}111) \\ (\bar{1}011) \\ (\bar{1}012)$
		(1010)

name	formula	schema
orthographic	$r = \sin \theta$	
equal angle (stereographic)	$r= anrac{ heta}{2}$	$(10\bar{1}0)$
gnonomic	r= an heta	$(01\overline{1}0) \qquad (11\overline{2}1) \qquad (2\overline{1}\overline{1}1) \qquad (1\overline{1}00) \\ (01\overline{1}1) \qquad (1\overline{1}01) \qquad (1\overline{1}01)$
equal area (Schmidt)	$\sqrt{2(1-\cos heta)}$	$(\overline{1}2\overline{1}1) \qquad (0001) \qquad (1\overline{2}11) \\ (\overline{1}101) \qquad (0\overline{1}11)$
equal distant	$r = \theta$	$(\bar{1}100) \qquad (\bar{2}111) \qquad (\bar{1}\bar{1}21) \qquad (0\bar{1}10)$
		$(\overline{1}010)$

name	formula	schema
orthographic	$r = \sin \theta$	
equal angle (stereographic)	$r= anrac{ heta}{2}$	(1121) (2111)
gnonomic	r= an heta	(10 <u>1</u> 1) (1 <u>1</u> 01)
equal area (Schmidt)	$\sqrt{2(1-\cos\theta)}$	$(\overline{1211}) \qquad (0001) \qquad (1\overline{211}) \\ (\overline{1101}) \qquad (0\overline{111}) \qquad (\overline{1011})$
equal distant	$r = \theta$	(2111) (1121)

name	formula	schema
orthographic	$r = \sin \theta$	
equal angle (stereographic)	$r= anrac{ heta}{2}$	(1010)
gnonomic	r= an heta	$(01\overline{1}0) \qquad (11\overline{2}1) \qquad (10\overline{1}1) \qquad (1\overline{1}00) \qquad (1\overline{1}01) \qquad (1\overline{1}01)$
equal area (Schmidt)	$\sqrt{2(1-\cos heta)}$	$(\overline{1211}) \qquad (0001) \qquad (1\overline{2}11) \\ (\overline{1}101) \qquad (0\overline{1}11)$
equal distant	$r = \theta$	$(\bar{1}1\bar{0}0) \\ (\bar{2}111) \\ (\bar{1}011) \\ (\bar{1}\bar{1}21) \\ (0\bar{1}10)$
		(1010)

name	formula	schema
orthographic	$r = \sin \theta$	
equal angle (stereographic)	$r= anrac{ heta}{2}$	$(10\bar{1}0)$
gnonomic	r= an heta	$(01\overline{1}0) \qquad (11\overline{2}1) \qquad (10\overline{1}1) \qquad (2\overline{1}\overline{1}1) \qquad (1\overline{1}00) \qquad (1\overline{1}01) \qquad ($
equal area (Schmidt)	$\sqrt{2(1-\cos heta)}$	$(\bar{1}2\bar{1}1) \qquad (0001) \qquad (1\bar{2}11) \qquad (\bar{1}101) \qquad (0\bar{1}11)$
equal distant	$r = \theta$	$(\bar{1}1\bar{0}0)$ $(\bar{2}111)$ $(\bar{1}\bar{0}11)$ $(\bar{1}\bar{1}21)$ $(0\bar{1}10)$
		(1010)

```
spherical projections: earea, edist, eangle, 3d
```

```
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha,
MarkerFaceAlpha
```

labels: label, fontSize, backgroundcolor,

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
```

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
```

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha,
MarkerFaceAlpha
```

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha,
MarkerFaceAlpha
combined plots: hold on, hold off, add2all
```

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha,
MarkerFaceAlpha
combined plots: hold on, hold off, add2all
multiple plots: nextAxis, newMTEXFigure, gcm
```

```
spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha,
MarkerFaceAlpha
combined plots: hold on, hold off, add2all
multiple plots: nextAxis, newMTEXFigure, gcm
labels: label, fontSize, backgroundcolor,
```

Data Plots

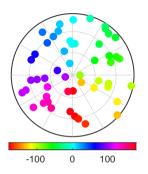
colorize vectors by value

```
v = vector3d.rand(100)
scatter(v,v.rho./degree)
mtexColorbar southoutside
mtexColorMap hsv
```

colorize by RGB triples

key = HSVDirectionKey
scatter(v, key.direction2color(v))

quiver(v, orth(v)) % a vector field



Data Plots

colorize vectors by value

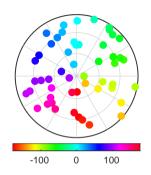
```
v = vector3d.rand(100)
scatter(v,v.rho./degree)
mtexColorbar southoutside
mtexColorMap hsv
```

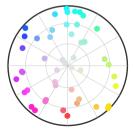
colorize by RGB triples

key = HSVDirectionKey scatter(v, key.direction2color(v))

visualize directions

quiver(v, orth(v)) % a vector field





Data Plots

```
colorize vectors by value
```

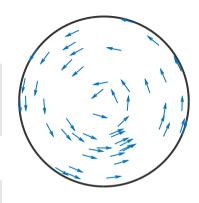
```
v = vector3d.rand(100)
scatter(v,v.rho./degree)
mtexColorbar southoutside
mtexColorMap hsv
```

colorize by RGB triples

key = HSVDirectionKey
scatter(v, key.direction2color(v))

visualize directions

quiver(v,orth(v)) % a vector field



Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

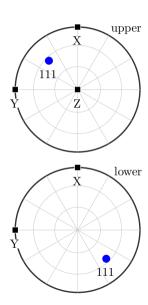
```
\mathsf{r} = \mathsf{vector3d}(1,1,1,'antipodal')
```

```
r = vector3d (show methods, plot)
size: 1 x 1
antipodal: true
x y z
1 1 1
```

Then r and -r represent the same axis

$$eq(r, -r)$$

The angle to an axis is always less then 90°



Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

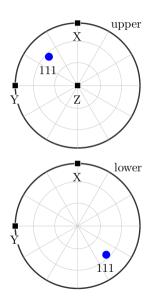
$$\mathsf{r} = \mathsf{vector3d}(1,1,1,'antipodal')$$

Then r and -r represent the same axis

$$eq(r, -r)$$

The angle to an axis is always less then 90°

$$angle(r,-vector3d.X) / degree$$



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$$\mathsf{r} = \mathsf{vector3d}(1,1,1,'antipodal')$$

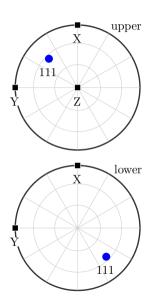
Then r and -r represent the same axis

$$eq(r, -r)$$

The angle to an axis is always less then 90°

angle(r,-vector3d.X) / degree

54.7



eq(r, -r)

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

```
\mathsf{r} = \mathsf{vector3d}(1,1,1,'antipodal')
```

Then r and -r represent the same axis

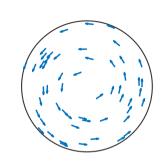
```
The angle to an axis is always less then 90^{\circ}
```

angle(r,-vector3d.X) / degree

angle (r, - vector su. x) / degree

Changing option antipodal

r = vector3d.rand(100) o = v.orth; quiver(v,o)



eq(r, -r)

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

```
\mathsf{r} = \mathsf{vector3d}(1,1,1,'antipodal')
```

Then r and -r represent the same axis

```
The angle to an axis is always less then 90^{\circ}
```

angle(r,-vector3d.X) / degree

Changing option antipodal

