# Matlab Basics and General Concepts of the MTEX Toolbox 

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2021

MTEX - A tool for calculating with orientation dependent properties

- crystal geometry
- EBSD data
$>$ grains, grain boundaries
- VRD data
- orientation distribution function
- texture simulations
- tensorial properties
- lastic / plastic deformation
- misorientations / twinning
* phase transformations
- parent grain reconstruction


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Focus: basics, generality, speed

## MTEX an Open Source Toolbox

## Large, well documented, tested

- 13 years of development
- 40000 lines of code, 33 percent comments
- 2000 downloads per version
- add-ons: MTEX GUI, MTEX2Gmsh, Stabix, CrystalAligner, phaseSegmenter


## A Teaching Tool

- everything can be visualized
- everything can be manipulated
- everything can be combined with everything


## Free and open software

- free to use
- free to modify
- very nice comunity

MTEX - A Matlab based scripting language

```
% load data
ebsd = EBSD.load('Emsland_plessite.ctf')
% plot data
plot(ebsd('Fe'), ebsd('Fe').orientations)
% reconstruct grains
th = 5*degree;
grains = calcGrains(ebsd, 'threshold',th)
% find largest grain
[m,id] = max(grains.area)
% plot largest grain
plot(grains(id).boundary,'linewidth',2)
```


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Why scripts?

- reproducible results
- easy to document
- templates for common tasks
- extensively customizable
- batch processing of many data sets
- repeated calculations with different parameters
Best practice
- comment your scripts
- short scripts
- function for repeated tasks
- avoid loops


## MTEX Resources

- documentation
- function reference
- examples
- user scripts
- discussion forum


## Matlab

## Three dimensional vectors

Three dimensional vectors are given by there coordinates with respect to a orthogonal coordinate system $\vec{X}, \vec{Y}, \vec{Z}$

$$
\vec{r}=x \cdot \vec{X}+y \cdot \vec{Y}+z \cdot \vec{Z}
$$

For general vectors, MTEX does not care about the coordinate system, but works only with the coordinates.
vector $3 \mathrm{~d}(1,2,3)$

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For general vectors, MTEX does not care about the coordinate system, but works only with the coordinates.

```
r = vector3d(1,2,3)
r = vector3d (show methods, plot)
    size: 1 x 1
    x y z
    123
```


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$$
r=\operatorname{vector} 3 \mathbf{d}(1,2,3)
$$

The alignment of the coordinate system is only important when plotting data

$$
\begin{aligned}
& \text { plotx2north, plotzOutOfPlane } \\
& \text { plot }(r)
\end{aligned}
$$



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$$
r=\operatorname{vector} 3 \mathbf{d}(1,2,3)
$$

The alignment of the coordinate system is only important when plotting data

## plotx2east, plotzOutOfPlane plot (r)



Only for directions relative to the crystal coordinate system the reference frame is considered.

## Defining vectors

predefined vectors
vector3d. X , vector3d. Y , vector3d. $Z$
polar coordinates $\vec{r}=(\sin \theta \cos \rho, \sin \theta \sin \rho, \cos \theta)^{t}$
theta $=90 *$ degree; rho $=45 *$ degree
$r=$ vector3d.byPolar(theta, rho)
In MTEX all angles are in radiant!
combine vectors
$r=[$ vector3d.X, vector3d.Y, vector3d $(1,1,1)]$
importing vectors
vector3d.Ioad ('file', 'ColumnNames
random vectors
vector3d rand (100)

## Defining vectors

predefined vectors

## vector3d.X, vector3d.Y, vector3d.Z

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## combine vectors

$r=[$ vector3d.X, vector3d.Y, vector3d(1,1,1)]

## importing vectors

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## Defining vectors

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combine vectors

```
r = vector3d (show methods, plot)
    x y z
    10}
    0 1 0
    1 1 1
```

$r=[v e c t o r 3 d . X, ~ v e c t o r 3 d . Y, ~ v e c t o r 3 d(1,1,1)]$

## Defining vectors

predefined vectors
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```
r = [vector3d.X, vector3d.Y, vector3d(1,1,1)]
```

importing vectors

```
r = vector3d.load('file','ColumnNames',{ 'x','y','z'})
```

```
r = vector3d (show methods, plot)
```


## Defining vectors

predefined vectors
vector3d. $X$, vector3d. $Y$, vector3d. $Z$
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combine vectors
$r=[v e c t o r 3 d . X$, vector3d.Y, vector3d(1,1,1)]
importing vectors

random vectors
$r=v e c t o r 3 d . r a n d(100)$

## Vector Calculations

simple algebra
$r=2 *$ vector3d. $X-$ vector3d. $Y$;
basic operations
$\boldsymbol{\operatorname { d o t }}(\mathrm{v} 1, \mathrm{v} 2) \quad \%$ dot product
cross(v1,v2) \% cross product
angle(v1,v2) \% angle between two vectors
normalize ( v )
orth (v)
extract properties
\% polar angle in radiant
\% azimuth angle in radiant

## Vector Calculations

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basic operations

```
dot(v1,v2) % dot product
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angle(v1,v2) % angle between two vectors
normalize(v) % scale to norm 1
orth(v) % arbitrary orthogonal vector
```


## extract properties

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orth(v) % arbitrary orthogonal vector
```

extract properties

```
r.theta % polar angle in radiant
r.rho % azimuth angle in radiant
r.x, r.y, r.z
```


## Indexing of Vectors

consider a list of vectors

```
r = vector3d([0 0 0 1 1],[[1 0 1 1 1],[[1 1 1 1 0]);
r = vector3d (show methods, plot)
    size: 1 x 4
    x y z
    0}11
    0}00
    1 1 1
    1 0
```

single out the second vector
single out the second and the fourth vector

## Indexing of Vectors

consider a list of vectors
$r=\operatorname{vector} 3 \mathbf{d}\left(\left[\begin{array}{llll}0 & 0 & 1 & 1\end{array}\right],\left[\begin{array}{llll}1 & 0 & 1 & 1\end{array}\right],\left[\begin{array}{llll}1 & 1 & 1 & 0\end{array}\right]\right)$;
single out the second vector
r (2)

```
r = vector3d (show methods, plot)
    size: 1 x 1
    x y z
    0}0
```

single out the second and the fourth vector
$\left.r\left(\begin{array}{ll}{[2} & 4\end{array}\right]\right)$
single out vectors by a logical condition
$x>0$ )

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single out the second vector
$r(2)$
single out the second and the fourth vector
$\left.r\left(\begin{array}{ll}2 & 4\end{array}\right]\right)$

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single out the second vector
$r(2)$
single out the second and the fourth vector
r ([ $\left.\begin{array}{ll}2 & 4\end{array}\right]$ )
single out vectors by a logical condition
$r(r . x>0)$

```
r = vector3d (show methods, plot)
    size: 1 x 2
    x y z
    1 1 1
    1 0
```


## Indexing of Vectors

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single out the second vector
$r(2)$
single out the second and the fourth vector
r([lll $\left.\left.\begin{array}{ll}2 & 4\end{array}\right]\right)$
single out vectors by a logical condition
$r(r . x>0)$
The above techniques applies also to lists of rotations, orientations, tensors, EBSD data, grains, boundary segments, triple points, etc.

## Changing Vectors

consider again the list of vectors
$r=\operatorname{vector} 3 d\left(\left[\begin{array}{llll}0 & 0 & 1 & 1\end{array}\right],\left[\begin{array}{llll}1 & 0 & 1 & 1\end{array}\right],\left[\begin{array}{llll}1 & 1 & 1 & 0\end{array}\right]\right)$;
$r=$ vector3d (show methods, plot)
size: 1 x 4
x y z
$\begin{array}{lll}0 & 1 & 1\end{array}$
$0 \quad 0 \quad 1$
$\begin{array}{lll}1 & 1 & 1\end{array}$
110
replace the second vector by another vector
$r(2)=$ vector3d $Y$
remove the second vector completely
$r(2)=[1$
change the $x$ coordinate of all vectors

## Changing Vectors

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replace the second vector by another vector

```
r(2) = vector3d.Y
r = vector3d (show methods, plot)
    size: 1 x 4
    x y z
    0}11
    0}11
    1}11
    1 0
```

remove the second vector completely

## Changing Vectors

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replace the second vector by another vector
$r(2)=\operatorname{vector} 3 d . Y$
remove the second vector completely
$r(2)=[]$

```
r = vector3d (show methods, plot)
    size: 1 x 3
    0 1 1
    1 1 1
    1 1 0
```


## Changing Vectors

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replace the second vector by another vector
$r(2)=\operatorname{vector} 3 d . Y$
remove the second vector completely
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change the $\times$ coordinate of all vectors
$r . x=0$

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replace the second vector by another vector
$r(2)=$ vector3d.Y
remove the second vector completely
$r(2)=[]$
change the $\times$ coordinate of all vectors
$r . x=0$
The above techniques applies also to pole figure data, orientations, EBSD data, grains, etc.

## Spherical Projections

spherical polar coordinates
$(x, y, z)=(\cos \rho \sin \theta, \sin \rho \sin \theta, \cos \theta)$
polar coordinates in the plane

$$
(x, y)=(r \cos \rho, r \sin \rho)
$$



## Spherical Projections



## Spherical Projections



## Spherical Projections



## Spherical Projections



## Spherical Projections



## Spherical Plots in MTEX

spherical projections: earea, edist, eangle, 3d
spherical region: upper, lower, complete, fundamentalRegion
plot alignment: plotx2east, plotx2north, plotzIntoPlane, plotzOutOfPlane
marker: s, d, o, v
markerSize, markerEdgeColor, markerFaceColor, linewidth, MarkerEdgeAlpha, MarkerFaceAlpha
combined plots: hold on, hold off, add2all
multiple plots: nextAxis, newMTEXFigure, gcm
labels: label, fontSize, backgroundcolor,

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labels: label, fontSize, backgroundcolor,

## Data Plots

colorize vectors by value
$\mathrm{v}=$ vector3d.rand(100)
scatter (v, v.rho./degree) mtexColorbar southoutside mtexColorMap hsv

## colorize by RGB triples


key $=$ HSVDirectionKey
scatter (v, key.direction2color (v))
visualize directions
ouiver (v, orth(v)) \% a vector field

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## visualize directions

quiver(v orth(v)) \% a vector field


## Data Plots

colorize vectors by value

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v = vector3d.rand(100)
scatter(v,v.rho./degree)
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```

colorize by RGB triples
key $=$ HSVDirectionKey
 scatter (v, key. direction2color (v))
visualize directions
quiver(v, orth(v)) \% a vector field

## Axes

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

```
r = vector3d(1,1,1,'antipodal')
r = vector3d (show methods, plot)
    size: 1 x 1
    antipodal: true
    x y z
    1 1 1
```

Then $r$ and $-r$ represent the same axis

## eq'r

The angle to an axis is always less then 90


## Axes

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

```
r = vector3d(1,1,1,'antipodal')
```

Then $r$ and -r represent the same axis

```
eq(r, -r)
```

| 1

The angle to an axis is always less then 90 angle(r, Uector3d $X$ ) / degree


## Axes

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

```
r = vector3d(1,1,1,'antipodal')
```

Then $r$ and $-r$ represent the same axis

$$
\| \mathbf{e q}(r,-r)
$$

The angle to an axis is always less then $90^{\circ}$

```
angle(r,-vector3d.X) / degree
```

54.7


## Axes

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

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```

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$$

The angle to an axis is always less then $90^{\circ}$
 |angle ( $r$, - vector ld. $X$ ) / degree

Changing option antipodal

```
r = vector3d.rand(100)
o = v.orth;
quiver(v,o)
```


## Axes

Axes are three dimensional vectors where we do not care about length and direction, e.g. plane normals.

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```

Then r and -r represent the same axis

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\| \mathbf{e q}(r,-r)
$$

The angle to an axis is always less then $90^{\circ}$

|angle(r,-vector3d.X) / degree

Changing option antipodal

```
r = vector3d.rand(100)
o = v.orth;
o.antipodal = true;
quiver(v,o)
```



