



Structure Formation - From a Cloud of Atoms to a Crystal -

(T11) On the medium-range order in alloys of aluminum with transition metals

H. Solbrig

1. spd electron phases
2. α -AlMnSi
3. i-AlCuFe (1/1)
4. Conclusions

1. spd electron phases

2. α -AlMnSi

3. i-AlCuFe (1/1)

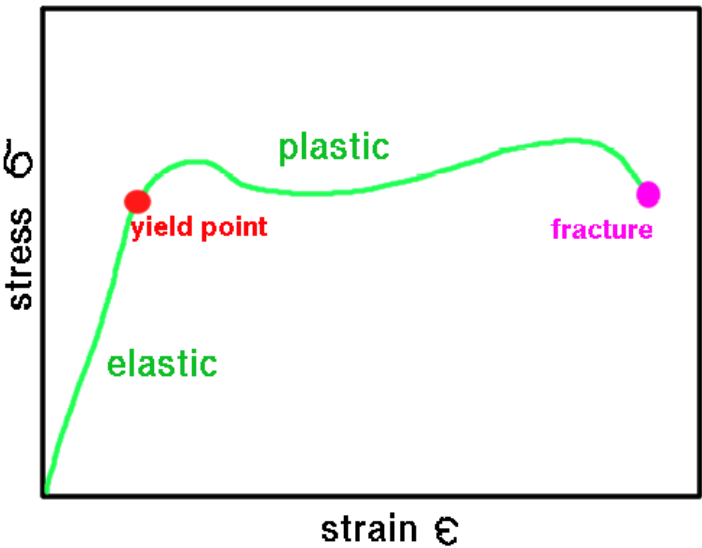
4. Conclusions

Mechanical properties and the valence electrons

attributes

strong	concrete
hard	diamond
brittle	rock salt
soft	sodium
elastic	a spring
ductile	aluminum
plastic	polymer

applying strain



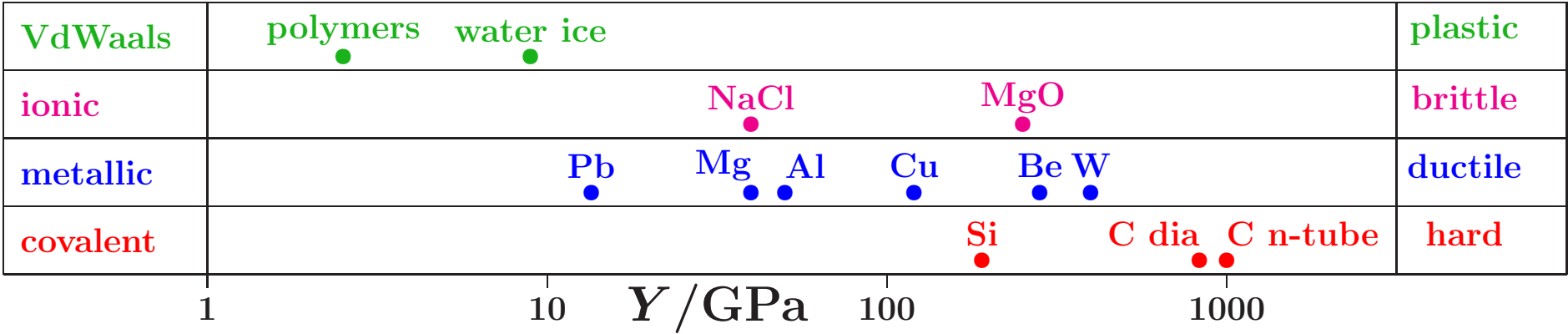
Hook’s law

in the elastic range:

$$\sigma = Y \epsilon$$

Young modulus

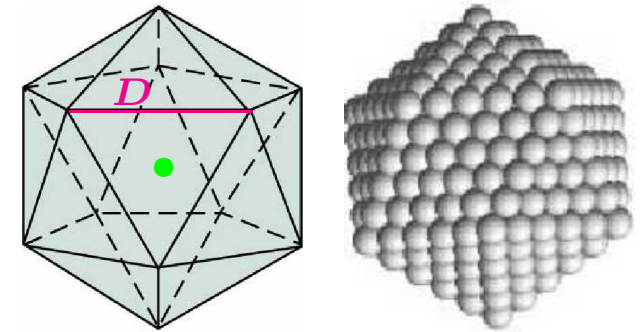
typical ranges of the Young modulus



Icosahedral clusters in complex alloys

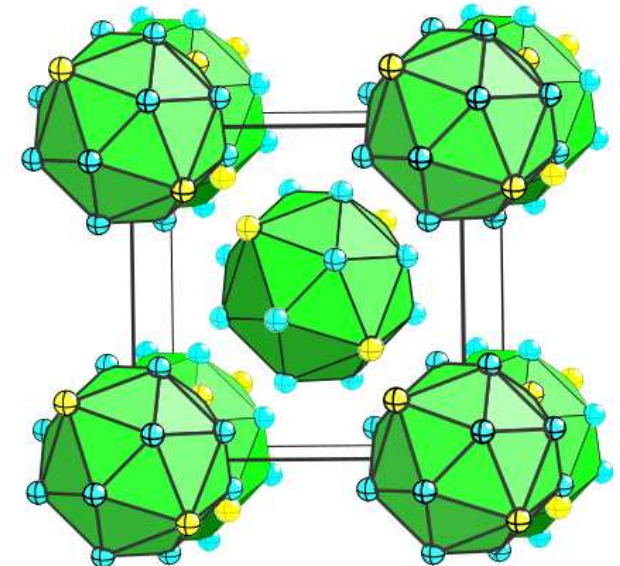
icosahedron: polyhedron(20 faces, 12 vertices, 30 edges)

- 12 vertices (spacing D)
on a sphere (radius $0.951 D$, center ●)
- **decorations** found with 12 or much more atoms
- **generated** by fast local relaxation,
space-filling arrangement avoided by fivefold symmetry



“cluster materials”: periodic arrangements of large complex clusters

e.g. bcc lattices of icosahedral clusters,
space between clusters filled with so-called “glue atoms”
(not shown)



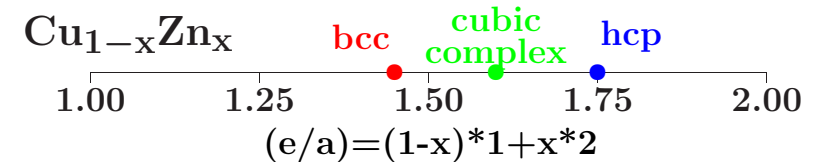
conclusion:

- subsystems contribute **hardness** or **ductility**

Concepts for electronic phase stabilization

order parameter for *sp* alloys:

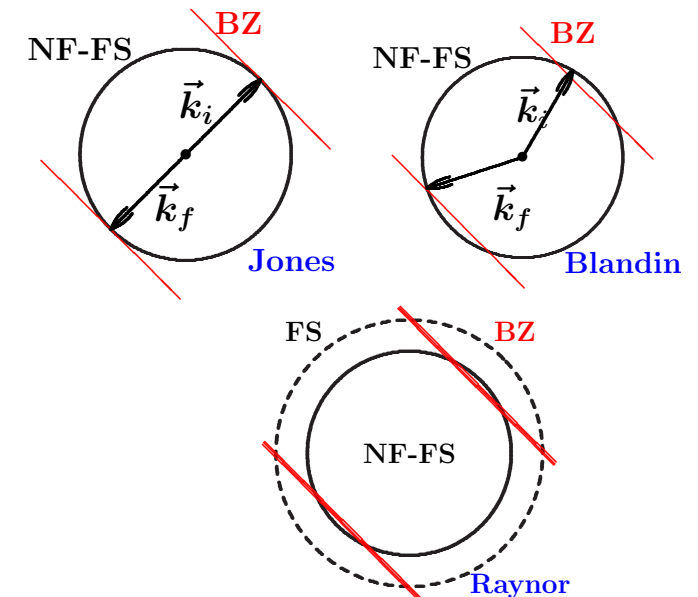
(*e/a*) controls structure (Hume-Rothery 1926)



diffraction picture:

nearly-free Fermi sphere **touches/cuts** a Brillouin zone

$\Rightarrow$ a pseudogap opens at ϵ_F (Jones 1937, Blandin 1965)



negative valence of transition metals (TM):

TM atoms **fill empty d orbitals**, carry negative charges

$\Rightarrow$ smaller nearly-free Fermi sphere (Raynor 1947)

amorphous Hume-Rothery phases:

main diffraction peak K_p close to $2k_F$

$\Rightarrow$ a pseudogap opens at ϵ_F (Nagel 1975, Häußler 1983)

virtual bound states model:

TM **impurity atom** in a *sp* matrix (e.g. Al)

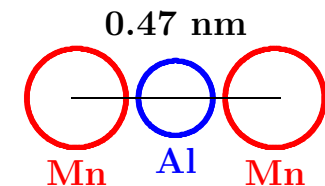
$\Rightarrow$ TM *d*-DOS has Lorentz profile, TM not charged

(Friedel 1956, Anderson 1961)

generalized to complex TM alloys with *d* resonances at ϵ_F

$\Rightarrow$ ***sp* neighbors** of TM atoms increase their *sp*-DOS below ϵ_F

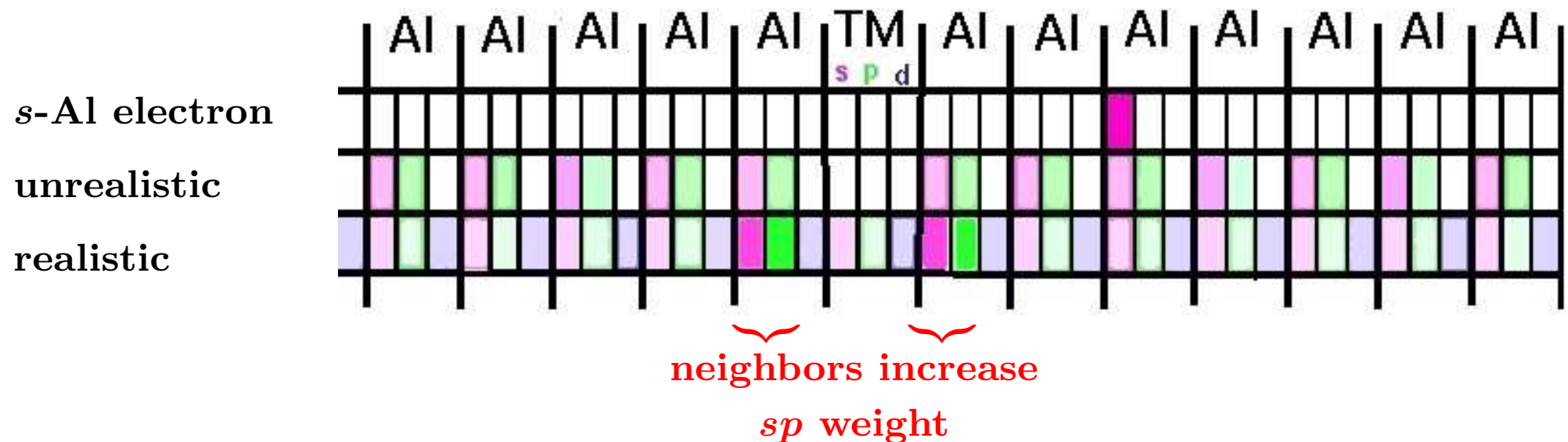
(Trambly de Laissardi re 1995)



sp-d hybridization

electronic band states are hybridized

$$|\nu\vec{k}\rangle = \sum_{sL}^{cell} \psi_{sL}(\nu\vec{k})|sL\rangle, \quad \sum_{sL}^{cell} |\psi_{sL}(\nu\vec{k})|^2 = 1$$



conclusions:

- Band states with considerable *sp*-Al/*d*-TM hybridization are **pinned** at TM atoms, are **less diffusive**, do **not belong** to the nearly-free Fermi sphere.
- The **negative TM valence** corresponds to the total increase of *sp* weight at **neighboring Al atoms**.

1. spd electron phases

2. α -AlMnSi

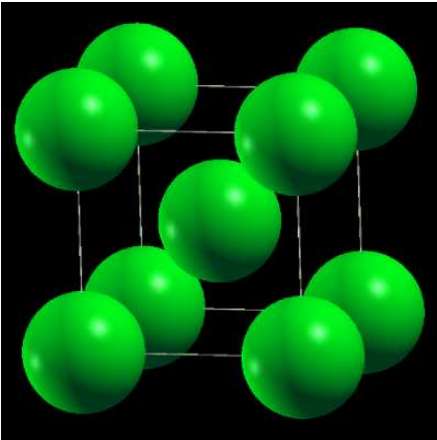
3. i-AlCuFe (1/1)

4. Conclusions

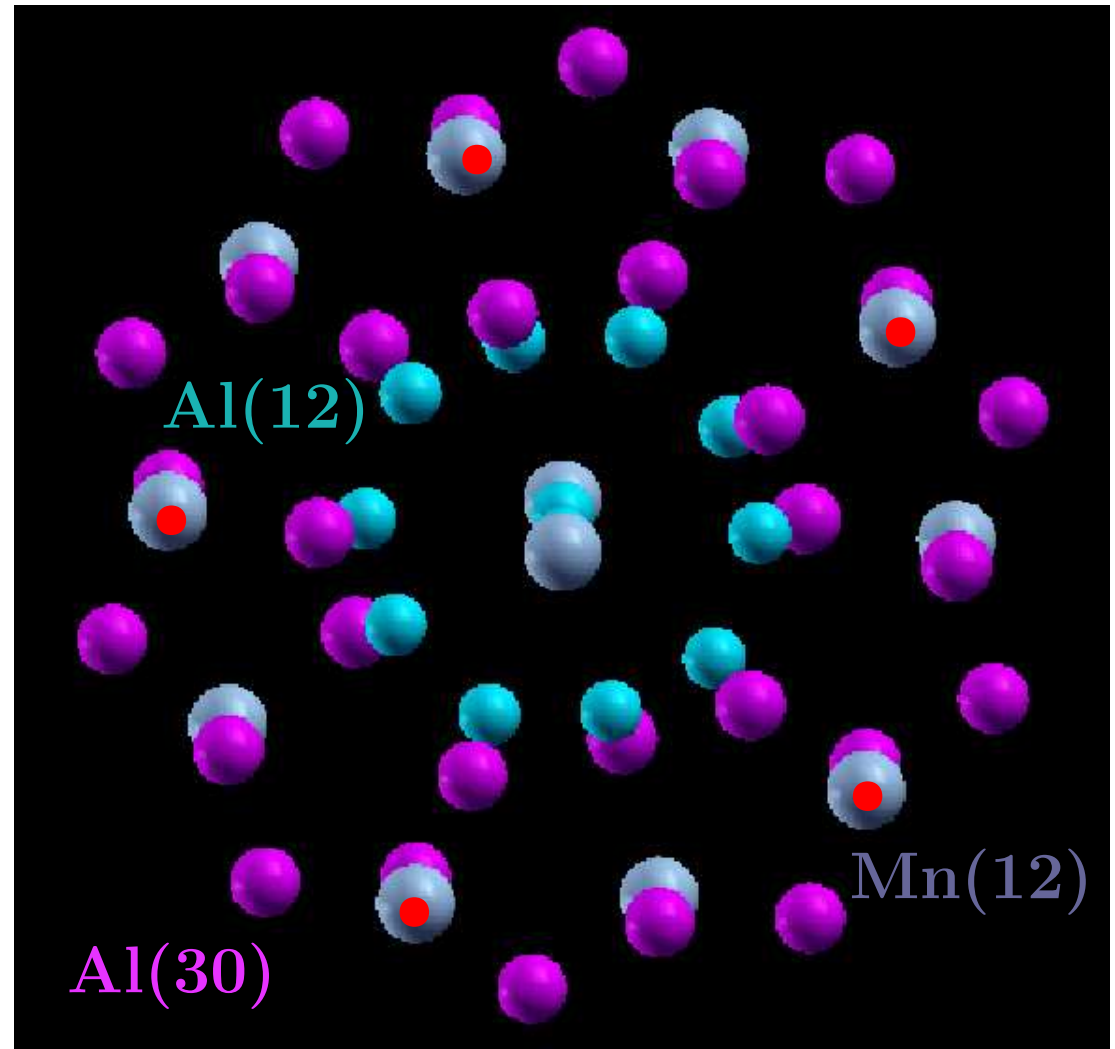
α -AlMn(Si): Mackay icosahedra

Elser-Henley model (1985)

bcc lattice of MI
and 30 Al glue atoms
(114 Al, 24 Mn)/cell



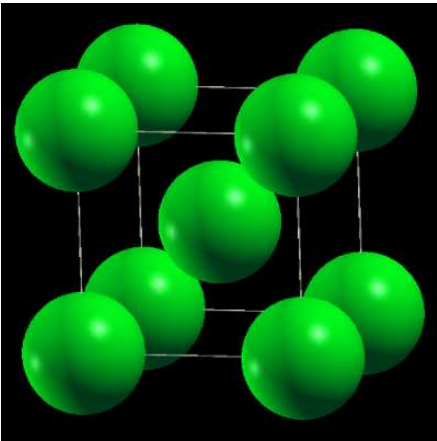
Mackay icosahedron (54 atoms)
center not occupied



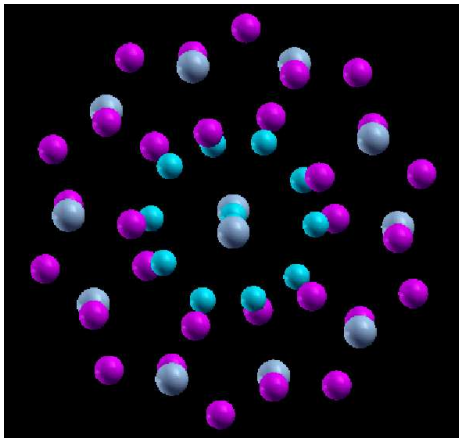
α -AlMn(Si): Planar Mn network

Elser-Henley model (1985)

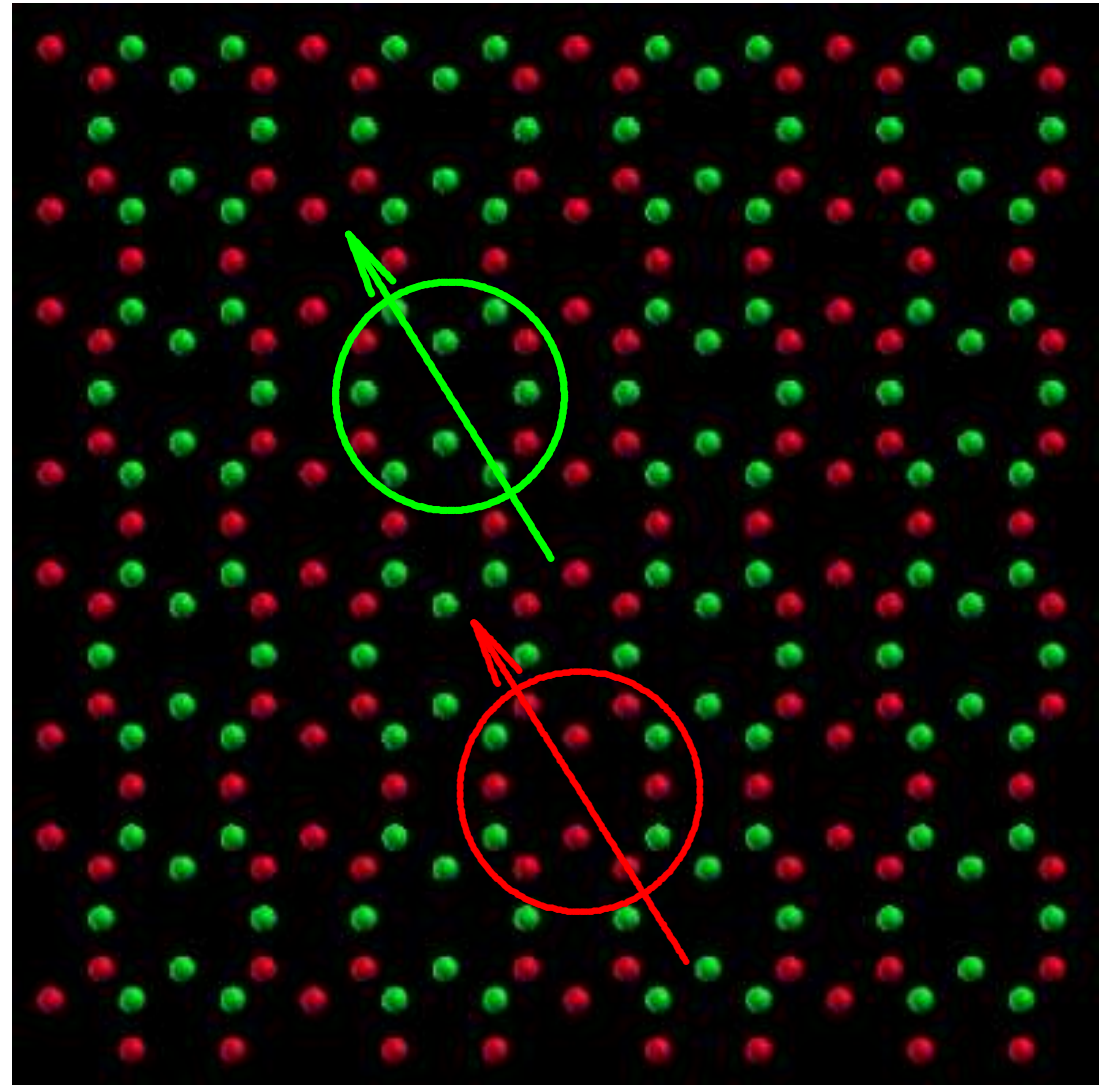
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Mackay icosahedron
1st shell (12 Al)
2nd shell (12 Mn, 30 Al)



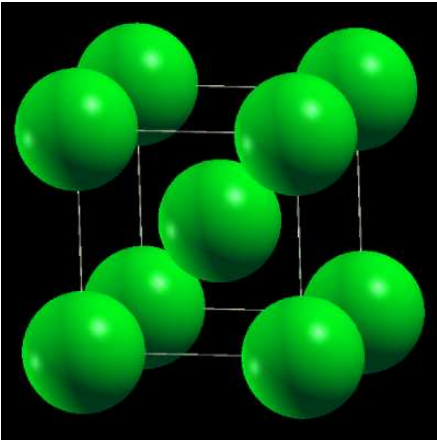
Mn planes configured by BCC + ICO
view along (010), Mn from 2 cubic MI-sublattices



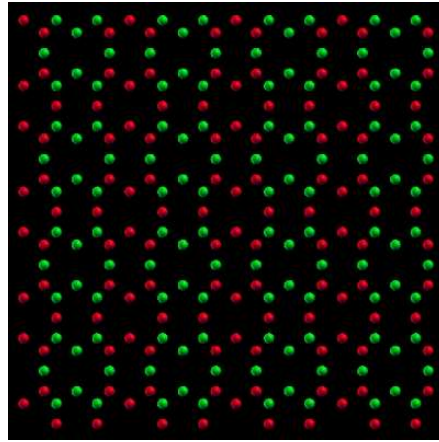
α -AlMn(Si): We disturb the planar order of Mn

Elser-Henley model (1985)

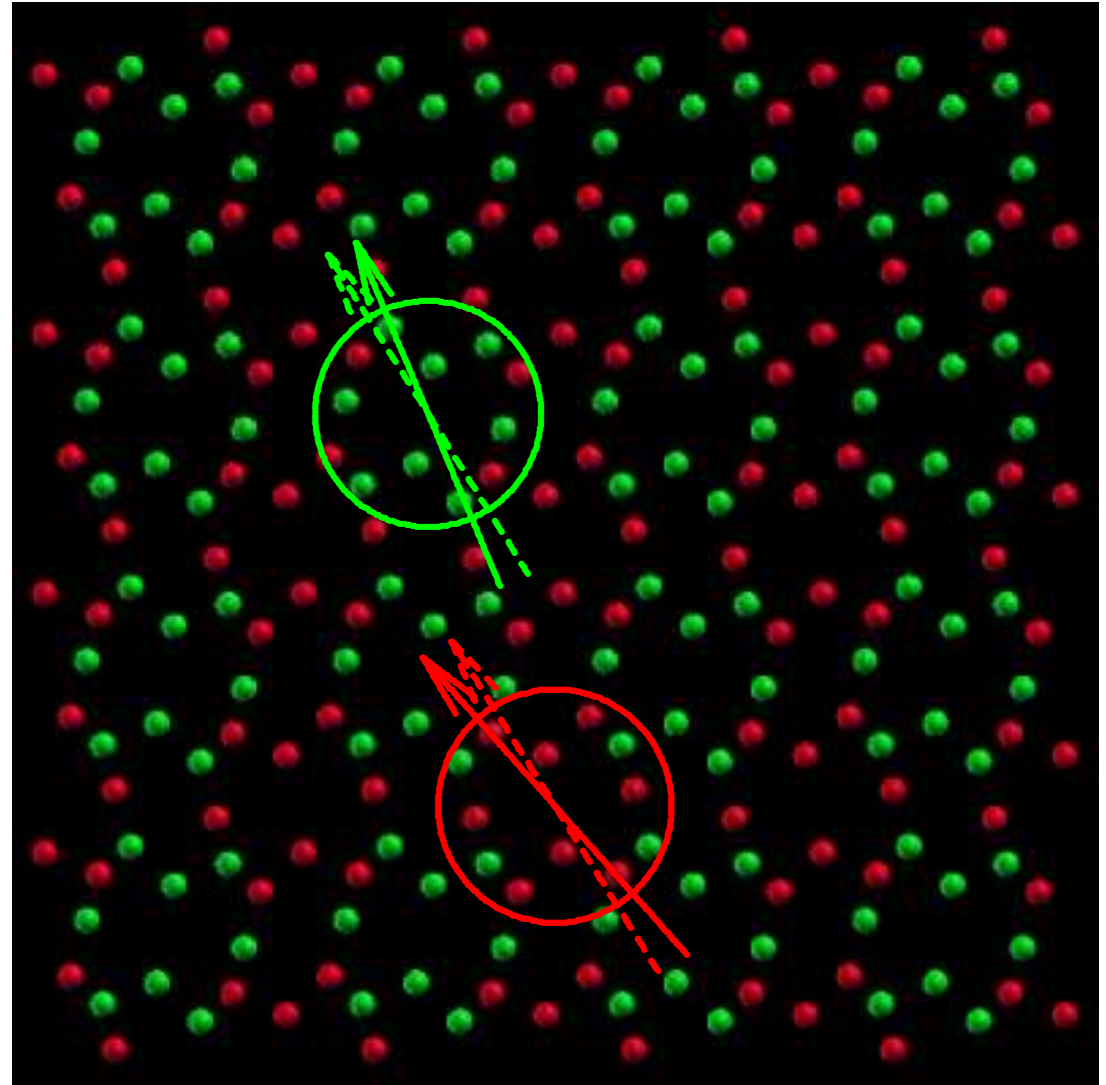
bcc lattice of MI
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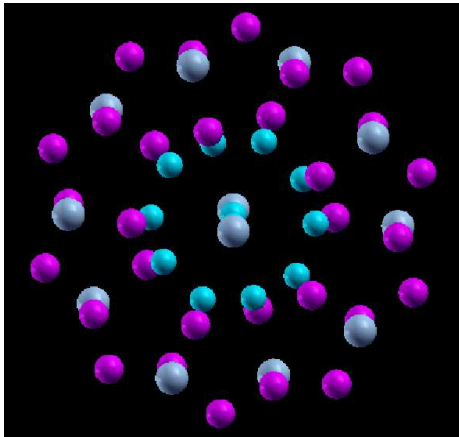
Mn planes configured
by BCC + ICO



rigid MI tilted $+10^\circ/-10^\circ$, axis (010)
planar order decays along (100) and (001)



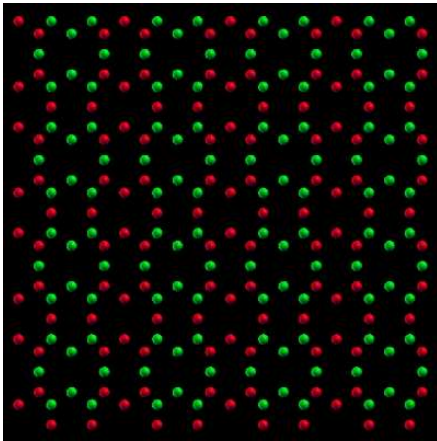
Mackay icosahedron
1st shell (12 Al)
2nd shell (12 Mn, 30 Al)



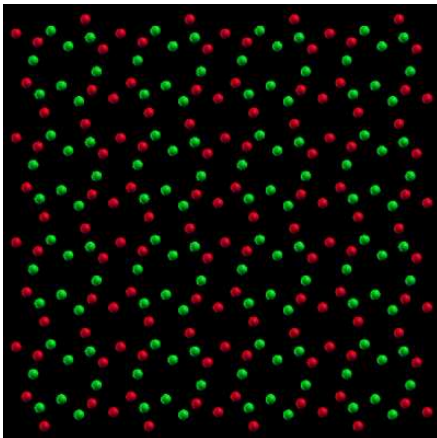
α -AlMn(Si): Does the structure factor change?

Elser-Henley model (1985)

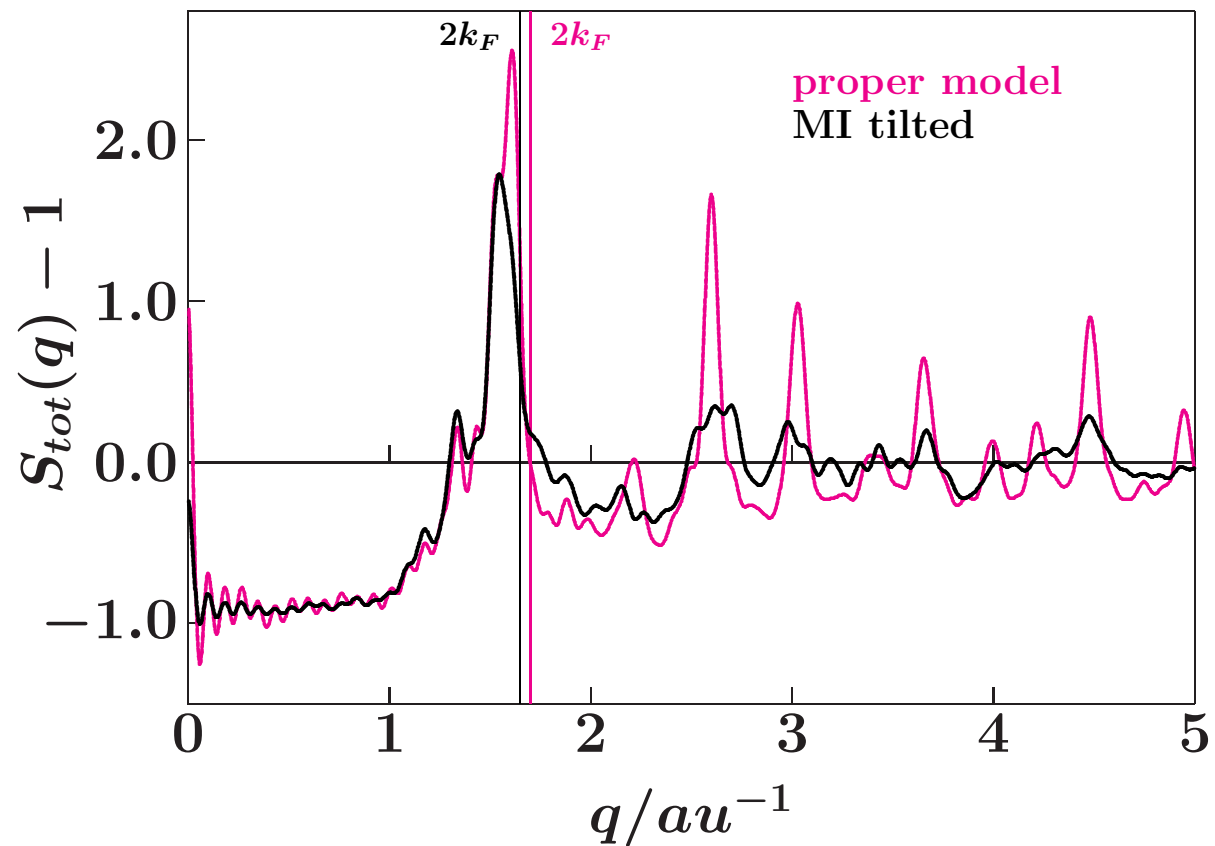
Mn planes configured
by BCC + ICO



with tilted MI
planar order decays



total structure factor



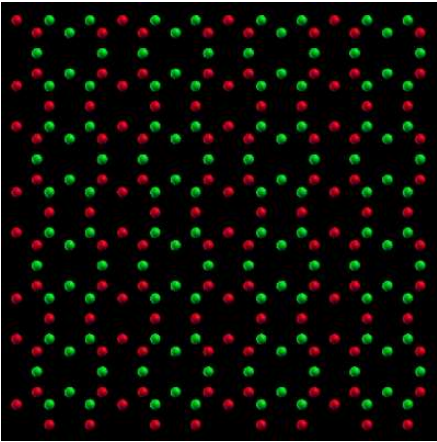
conclusion:

- main diffraction peak **less influenced**
 - $\Rightarrow$ neighbor-shell sequence also less influenced
 - $\Rightarrow$ s -DOS as well (expected)

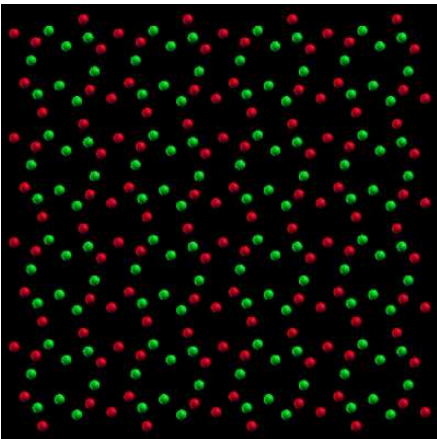
α -AlMn(Si): Does the electronic density of states change?

Elser-Henley model (1985)

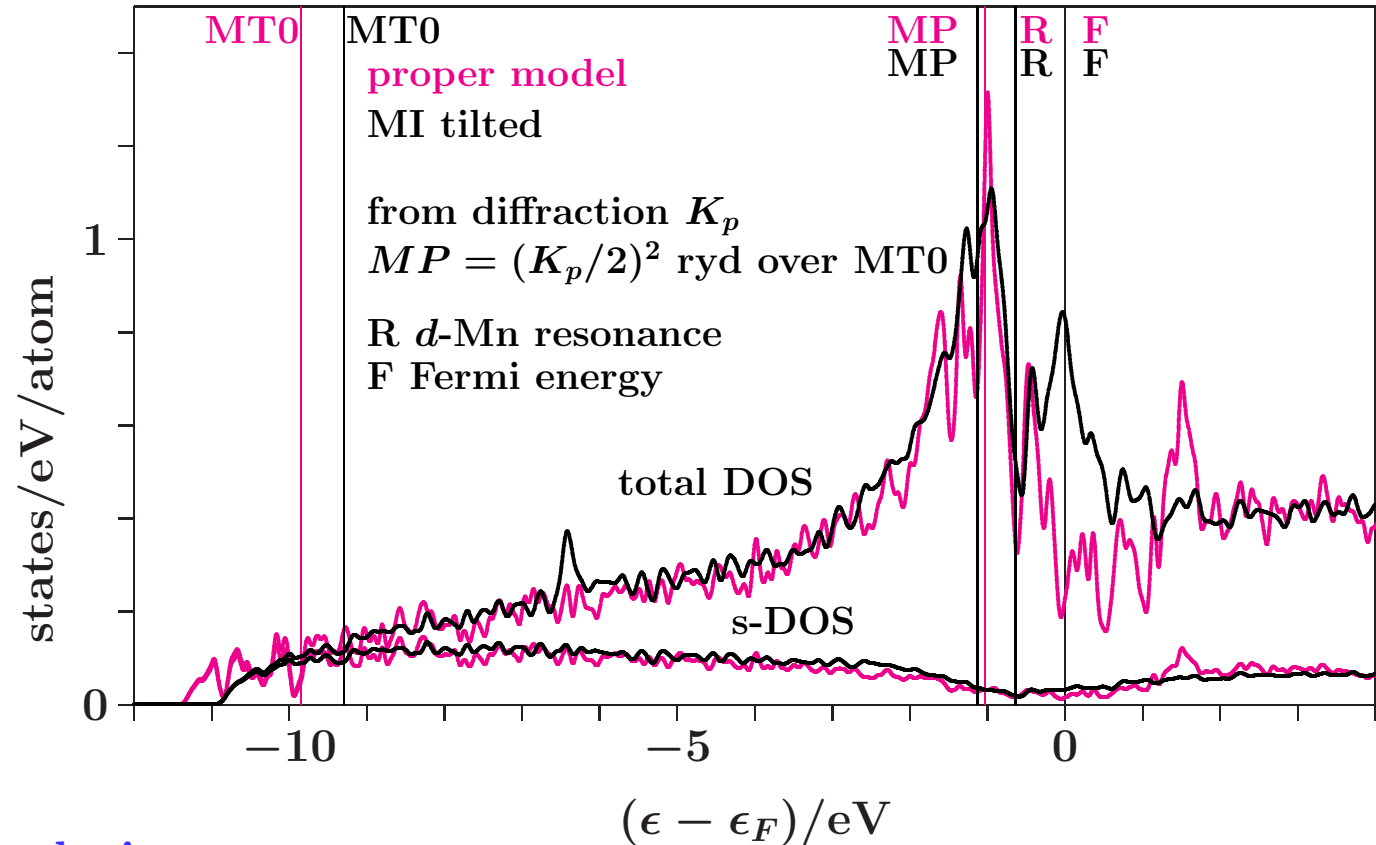
Mn planes configured
by BCC + ICO



with tilted MI
planar order decays



electronic density of states (DOS)



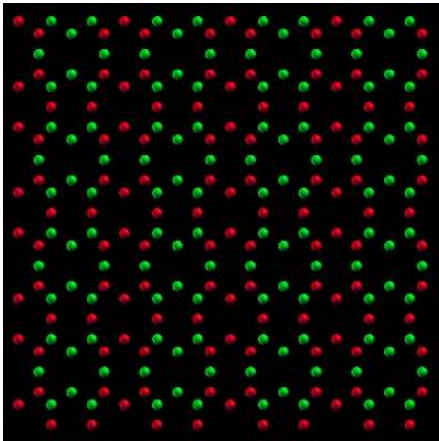
conclusions:

- Mn network **destabilized** (DOS peak at ϵ_F),
s-DOS (neighbor shell sequence) **not sensitive** about tilting MI
- two competing principles for stable atomic arrangements:
neighbor-shell order (weak *sp* scattering) and
network order (strong *d* scattering)

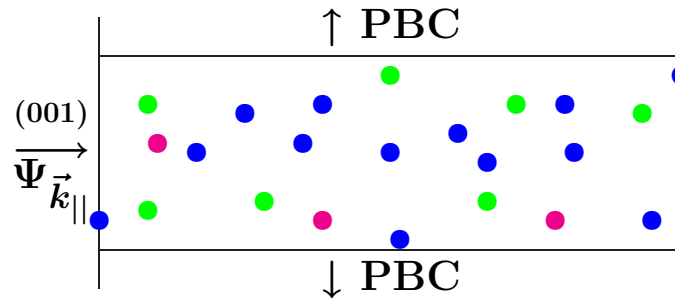
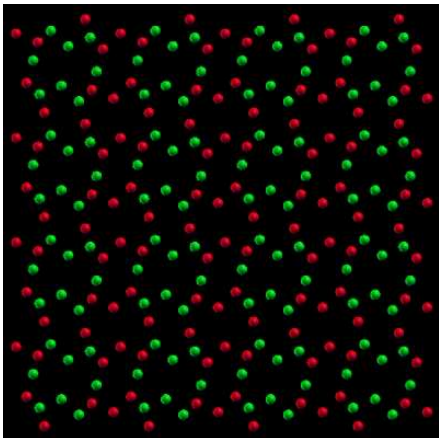
A slab of α -AlMn(Si): Does the resistance change?

Landauer resistance per unit area at ϵ_F (slab thickness 2.8 nm)

Mn planes configured
by BCC + ICO

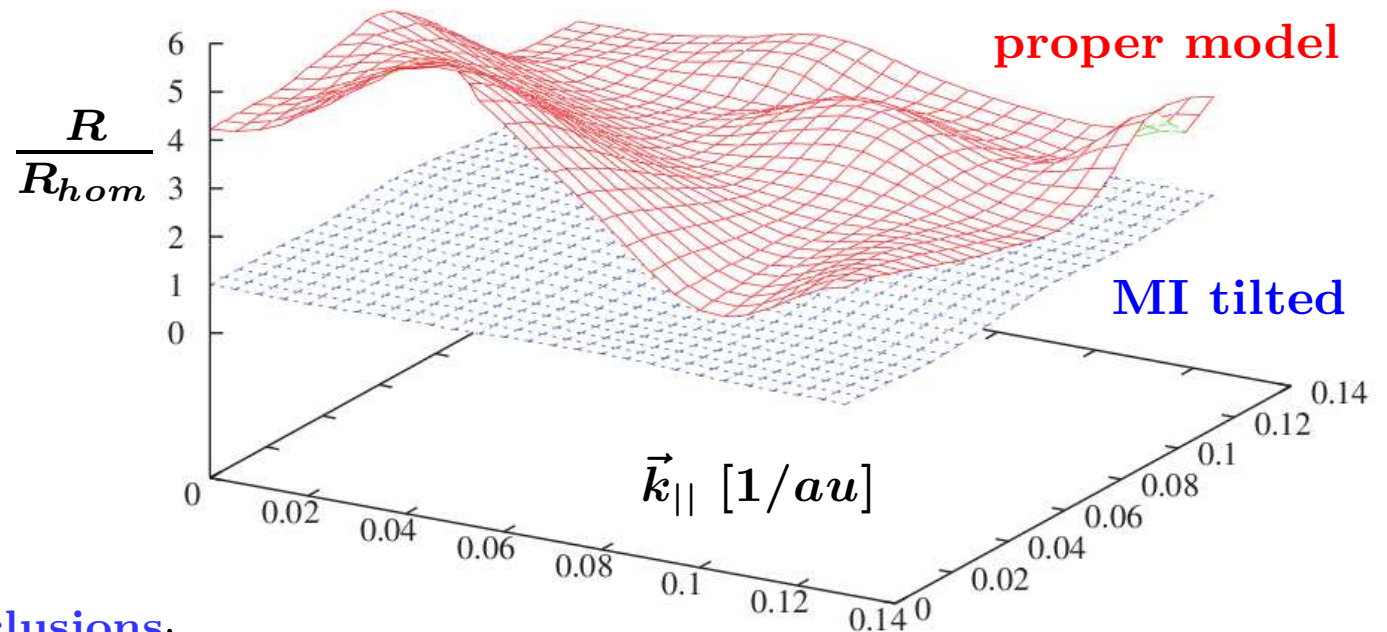


with tilted MI
planar order decays



$$\vec{t}(\epsilon, \vec{k}_{||}) \Psi_{\vec{k}_{||}} \quad R = \left[\frac{2e^2}{h} \text{Tr}(t^\dagger t) \right]^{-1}$$

reference system R_{hom} : homogeneous, $200 \mu\Omega\text{cm}$



conclusions:

- proper model: pronounced dependence on $\vec{k}_{||}$, **strong interference**
- after tilting MI: resembles a "**homogeneous**" material

1. spd electron phases

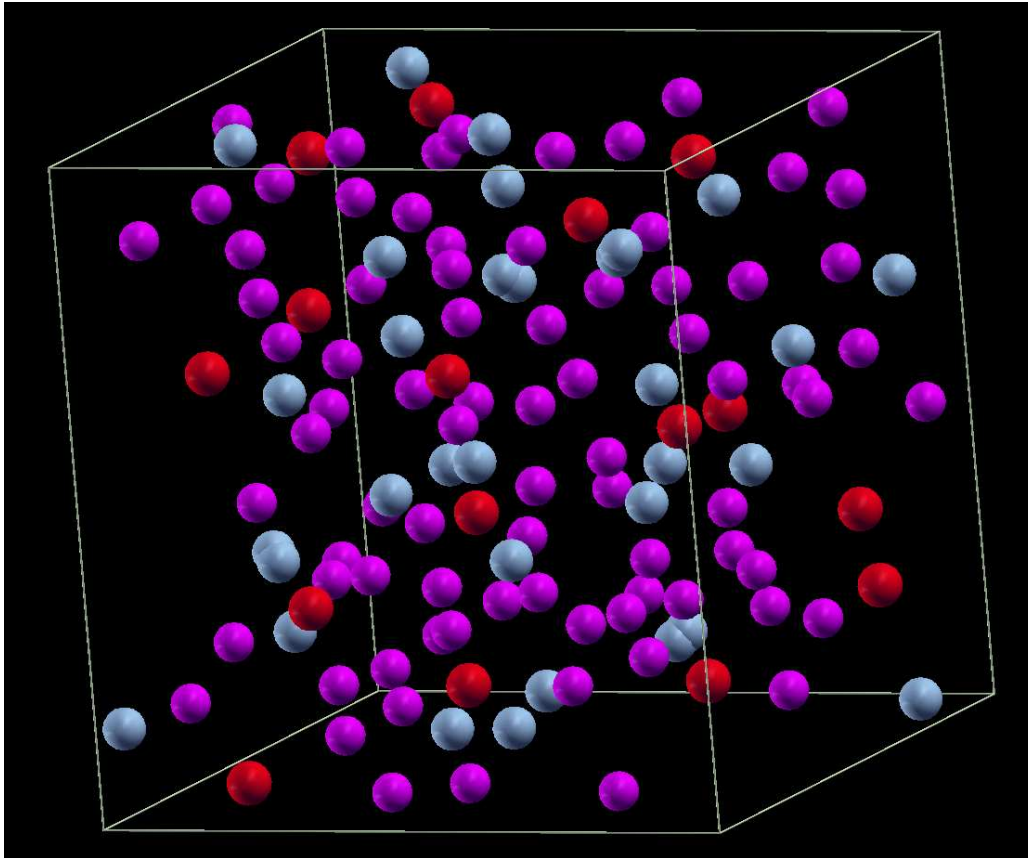
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4. Conclusions

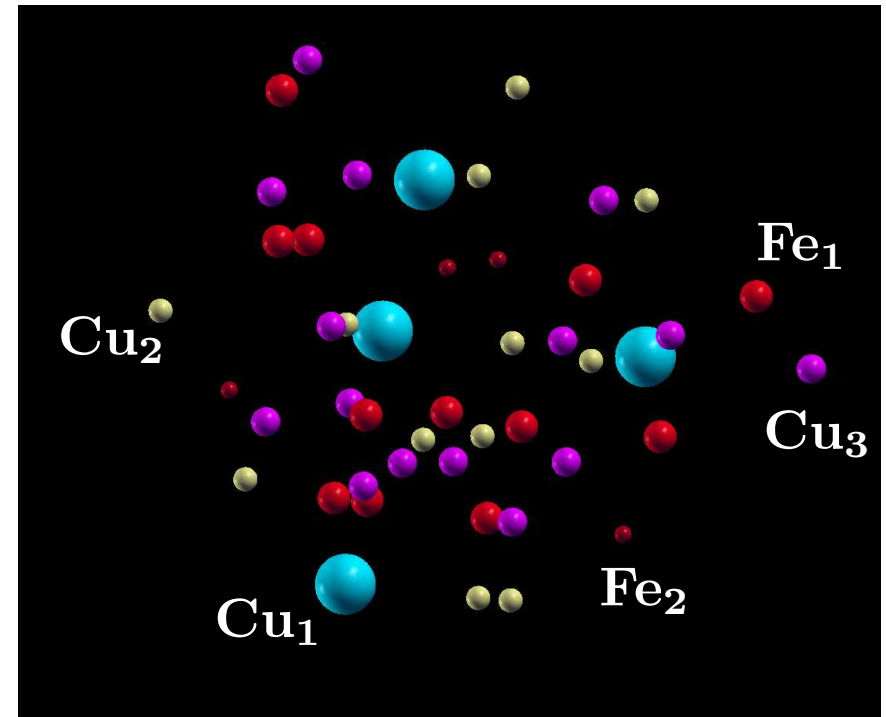
i-AlCuFe-(1/1): 13 types of effective atoms

Cockayne model (1993), the free-atom input:
128 atoms = 80 Al + 32 Cu + 16 Fe



due to **different** environments
different effective atoms:

8 types Al₁₋₈ (not shown) and
4 Cu₁, 12 Cu₂, 16 Cu₃ and
12 Fe₁, 4 Fe₂

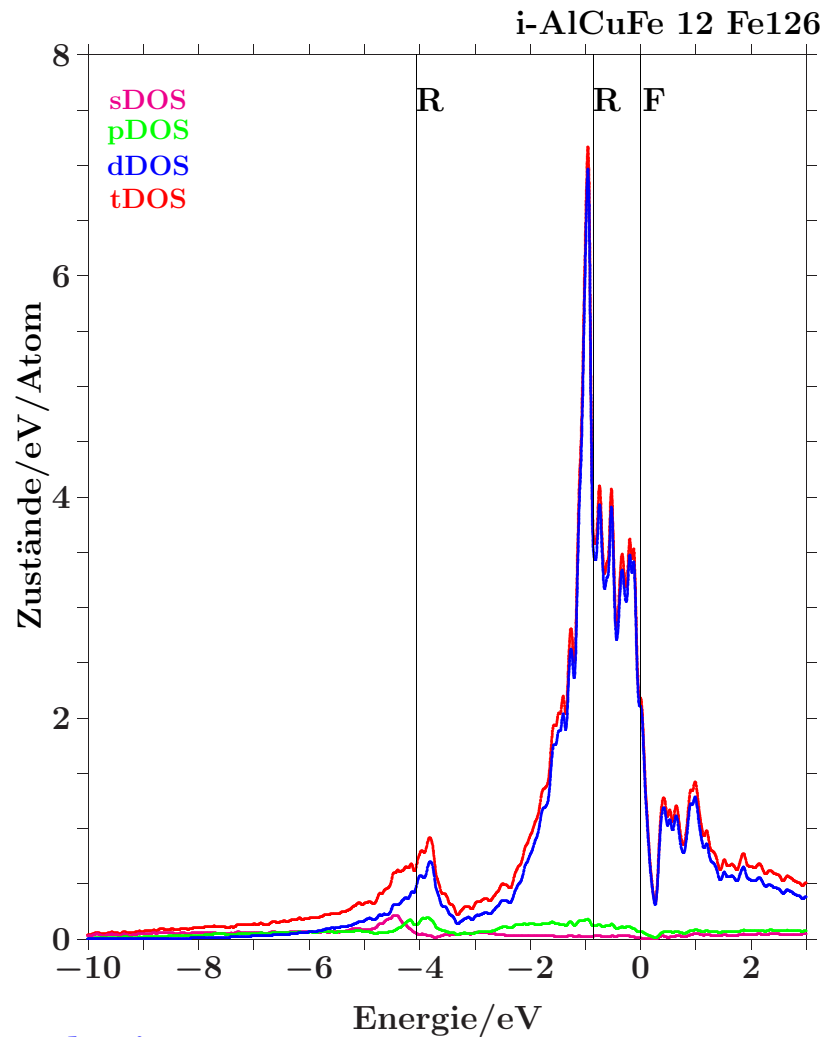


conclusion:

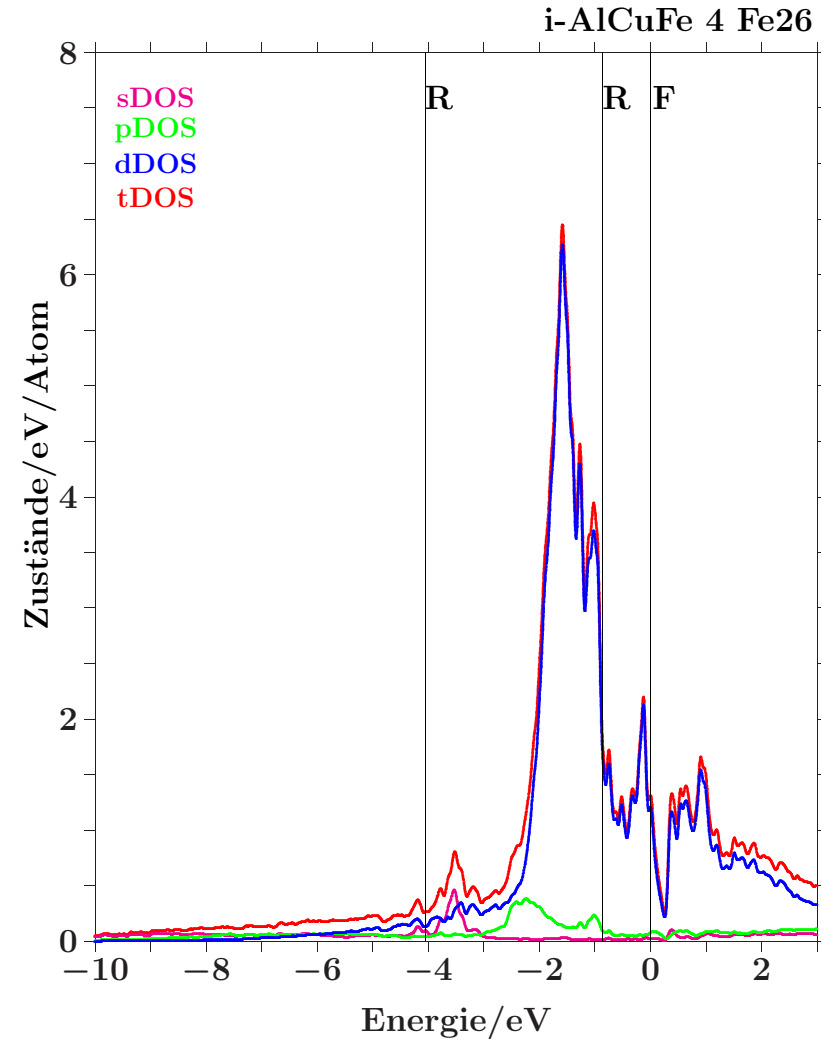
- Fe₁ **close to Cu** contrary to Fe₂

i-AlCuFe-(1/1): More Cu signature at Fe₁ than at Fe₂

DOS at Fe₁



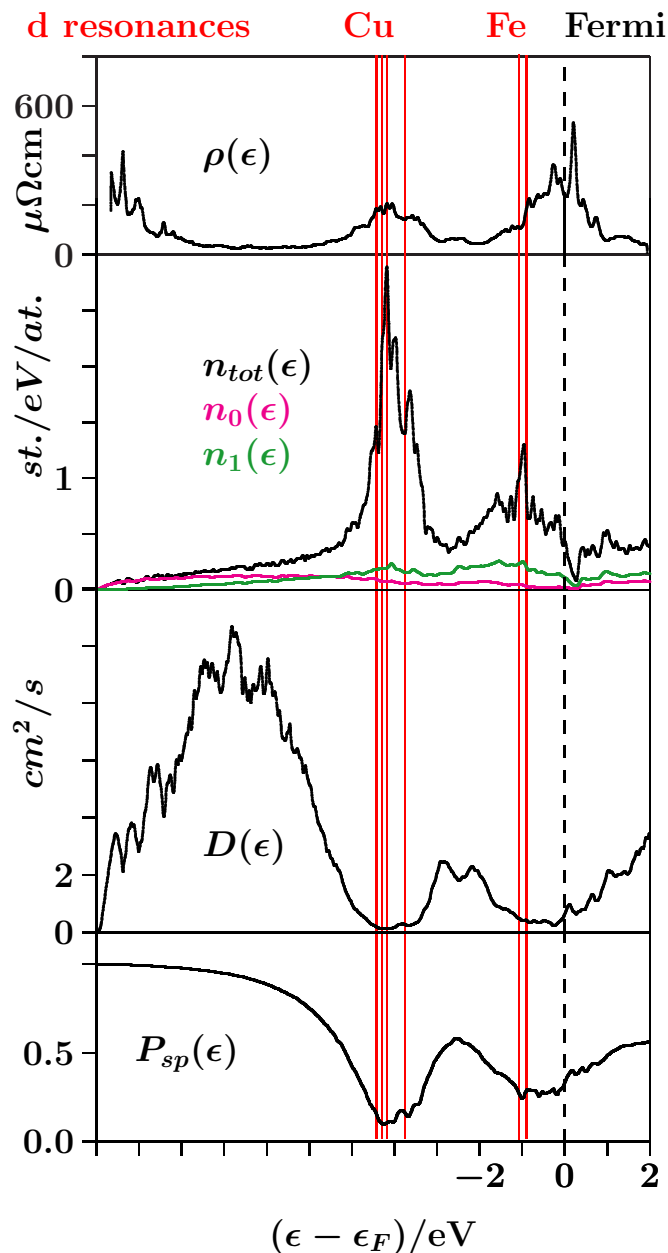
DOS at Fe₂



conclusion:

- note also: both Fe have **Fano profiles** at ϵ_F

i-AlCuFe-(1/1): Spectral curves



structure (Cockayne *et al.* 1993) 128 atoms

spectral resistivity $\rho(\epsilon)$

- 150-meV resistivity peak, thermally stable, aligned with DOS pseudogap

electronic density of states $n(\epsilon)$

- clear signatures of effective-atom d resonances
- Fano profile at ϵ_F

spectral diffusivity $D(\epsilon)$

- minimum diffusivity in the d -Cu band

sp content of band states $P_{sp}(\epsilon)$

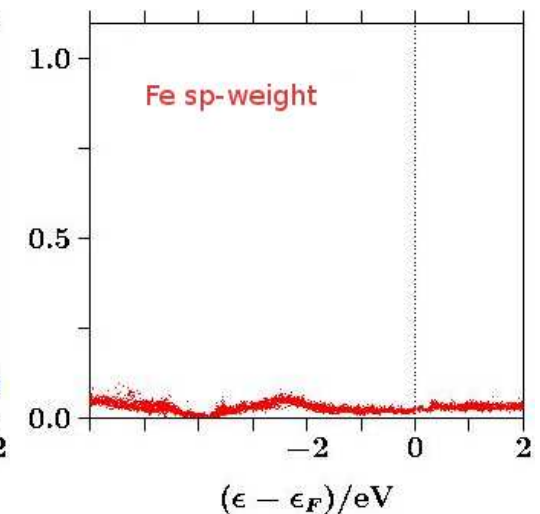
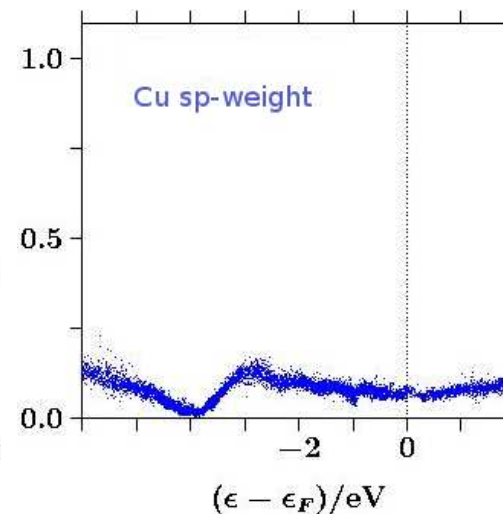
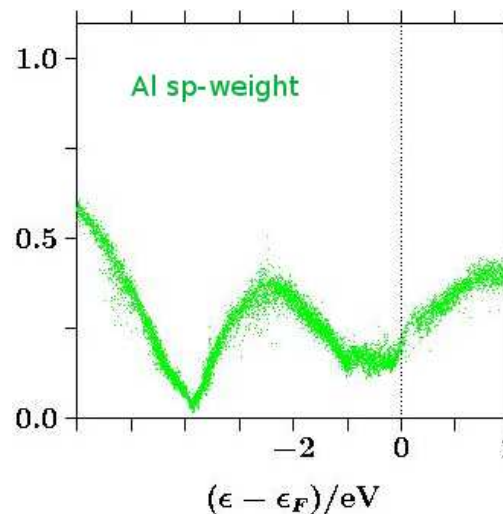
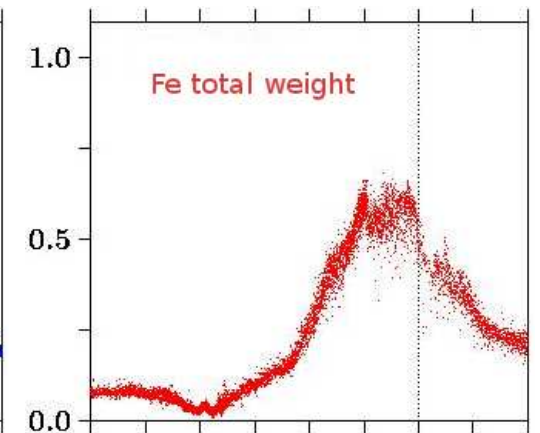
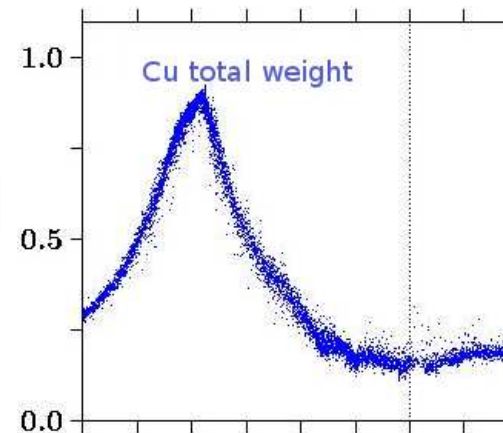
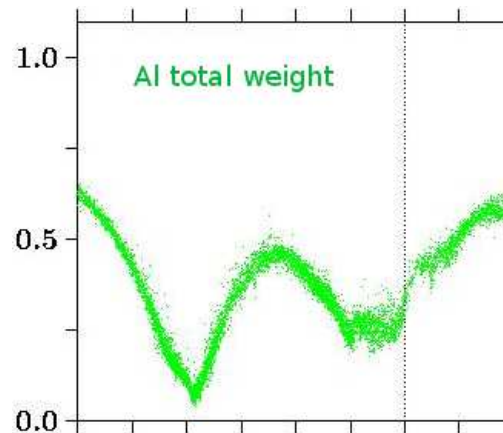
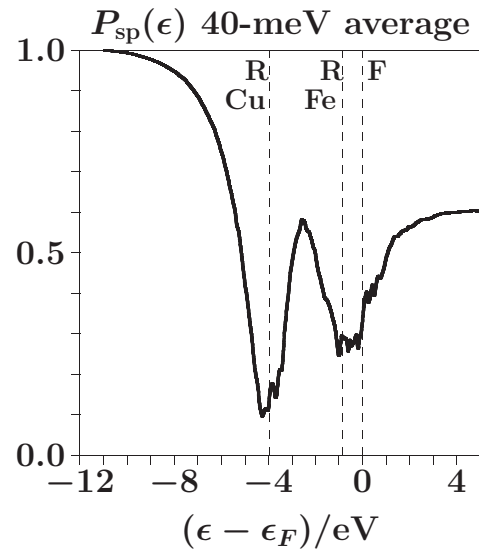
- in the d -Cu band almost pure d -Cu states

conclusion:

- pronounced **spectral fine structures** around ϵ_F

i-AlCuFe-(1/1): Decomposition of band states

hybridization status revealed: decomposition with respect to atom / angular momentum



for each band state
a dot

$$\sum_{sl}^{subset} \sum_{m=-l}^l |\psi_{slm}|^2$$

conclusion:

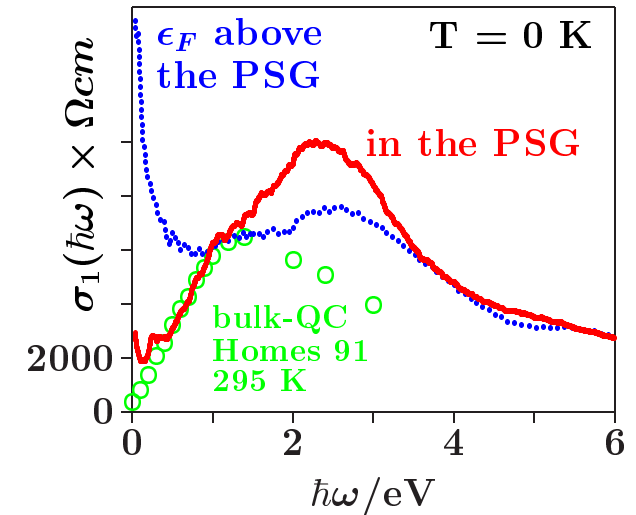
- note the **small fluctuation width** at given energy
- almost pure **d-Cu states** in the d-Cu band, below ϵ_F mainly **d-Fe** and **sp-Al**

i-AlCuFe (1/1): Really approximat of the i-AlCuFe QC ?

ϵ_F in a deep pseudogap (proof: optical conductivity without Drude peak)

$$\sigma_1(\hbar\omega) = \int d\epsilon \sigma(\epsilon, \epsilon + \hbar\omega) \frac{f^0(\epsilon) - f^0(\epsilon + \hbar\omega)}{\hbar\omega}$$

$$\overbrace{\frac{|e|^2 \hbar}{V} \sum_{ij} \langle i|v|j \rangle \langle j|v|i \rangle \delta(\epsilon - \epsilon_i) \delta(\epsilon + \hbar\omega - \epsilon_j)}$$

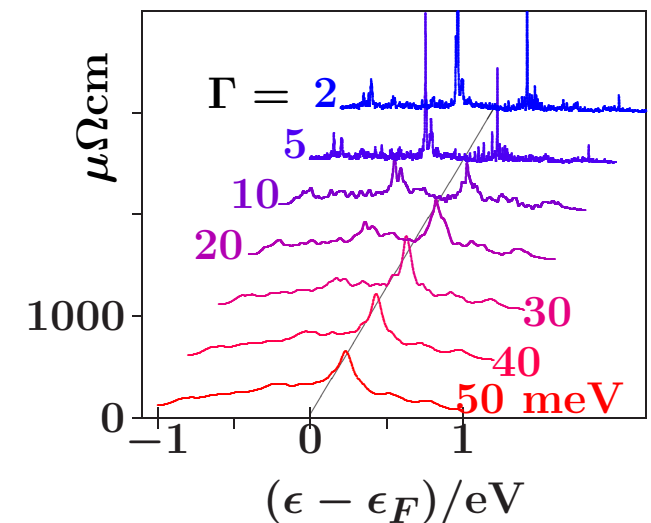


only one resistivity peak (pseudogap) is thermally stable

enhanced thermal collision

simulated by Gaussian level broadening (Γ)

scattering time $\tau \approx \frac{\hbar}{\Gamma}$



Scaling the spectral resistivity model of the approximant⁵

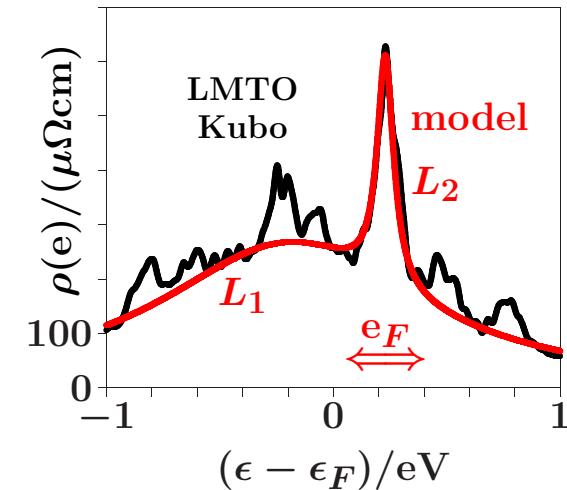
2 Lorentzians required for the Cockayne model

L_1 , width eV, atomic-scale processes

L_2 , width 100 meV, cluster-scale processes

$$\rho(\epsilon) = \sigma^{-1}(\epsilon) = A [L_1(\epsilon) + \alpha L_2(\epsilon)]$$

$$L_j(\epsilon) = \frac{\gamma_j/\pi}{[(\epsilon - (\epsilon_F + \delta_j))^2 + \gamma_j^2]}$$



fit A , α , γ_2 to approximate the measured thermopower $S^{exp}(T)$, ρ_{4K}^{exp}

Phase	ρ_{4K}^{exp} $\mu\Omega \text{ cm}$	$\frac{\alpha/\gamma_2}{1/\gamma_1}$	A $\mu\Omega \text{ cm eV}$	δ_1 eV	γ_1 eV	α	δ_2 eV	γ_2 meV
(1/1)-APP ¹	610	1.6	580	-0.2	0.7	0.1	0.23	44
thin film ²	2333	7.8	1047	-0.2	1.35	0.32	0.23	55
poly ³ Al ₆₃ Cu ₂₅ Fe ₁₂	4957	11	1400	-0.2	1	0.45	0.23	41
poly ³ Al ₆₂ Cu _{25.5} Fe _{12.5}	7241	31	1047	-0.2	1.35	0.98	0.23	43
bulk ⁴ Al _{62.5} Cu ₂₅ Fe _{12.5}	8078	34	1047	-0.2	1.35	1.0	0.23	40

¹ Cockayne *et al.* 93, ² C. Madel 00, ³ Bilušić *et al.* 01, ⁴ Pierce *et al.* 93, ⁵ Landauro *et al.* 01

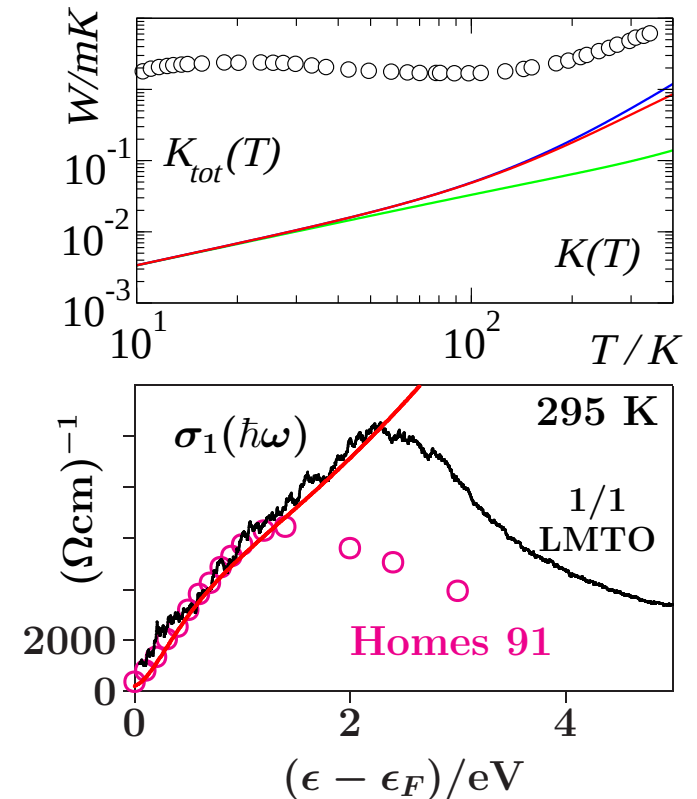
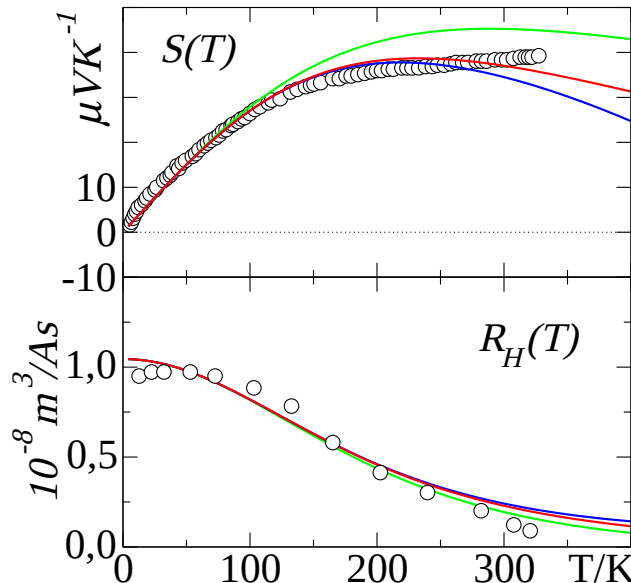
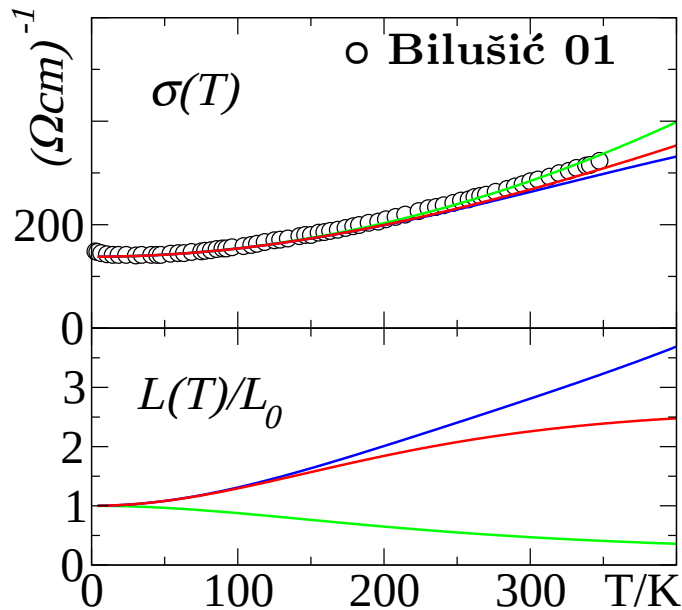
conclusion:

high 4K-resistivity if the **small** Lorentian predominates

Application to the poly-quasicrystal i-Al₆₂Cu_{25.5}Fe_{12.5}

elec. cond.	$\sigma(T) = \mathcal{L}^{11}(T)$	therm. cond.	$K(T) = \frac{\mathcal{L}^{22}(T)}{ e ^2 T} - T\sigma(T) S(T)^2$
thermopower	$S(T) = \frac{1}{ e T} \frac{\mathcal{L}^{12}(T)}{\sigma(T)}$	Lorenz number	$L(T) = \frac{K(T)}{T\sigma(T)}, L_0 = \left(\frac{k_B}{e}\right)^2 \frac{\pi^2}{3}$
Hall coefficient	$R_H(T) = \frac{ e }{\sigma(T)^2} \int d\epsilon \left(-1.13 \times 10^{-5} \text{Am}^2 \frac{d}{d\epsilon} \hat{\sigma}(\epsilon) \right) \left(-\frac{\partial f^0(\epsilon, \mu, T)}{\partial \epsilon} \right)$		

with kinetic coefficients $\mathcal{L}^{ij}$ integrated **numerically**, expanded up to T^4 or T^6



$$\hat{\sigma}(\epsilon, \epsilon + \hbar\omega) \approx 1.8 \sqrt{\hat{\sigma}(\epsilon) \hat{\sigma}(\epsilon + \hbar\omega)}$$

General Conclusions

Properties of complex alloys depend substantially on the
electron-ion interrelations
in the medium order range (nanometers).

Complex Al-TM alloys demonstrate that a general neighbor-shell order
can coexist
with a TM-based network order.

Shell order is mainly supported by
FE-like band electrons
whereas
***d*-TM hybridized** band electrons
support network order.

Shell order forms spectral structures on the
1-eV scale
whereas those on the
0.1-eV scale
are due to network order.